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An Analytical Equation of State for Molten Polymers

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Abstract

An analytical equation of state (EOS) developed by Ihm-Song-Mason (ISM) has been applied to calculate some thermophysical properties of molten polymers including Poly (1-octene) (PO), Poly (vinyl methyl ether) (PVME), Poly (vinyl chloride) (PVC), and Poly (styrene) (PS). Three temperature-dependent parameters of the ISM EOS have been determined based on the alternative scaling constants, dispersive energy parameters between segments/monomers (ε) and segment diameter (σ). The ability of the proposed EOS has been checked by comparing the results with 547 literature data points for the specific volumes over temperature from 311-557 K and pressure ranging from 0.1 up to 200 MPa. The average absolute deviation (AAD) of the calculated specific volumes from literature data was found to be 0.47%. The isothermal compressibility coefficients, κ_T have also been predicted using ISM EOS. From 188 data points examined, the AAD of estimated κ_T was equal to 7.75%. Our calculations on the volumetric and thermodynamic properties of studied polymers reproduce the literature data with reasonably good accuracy.

Keywords: Equation of state, Molten Polymers, thermodynamic properties

1. Introduction

Knowledge of the thermophysical properties of polymers is a prerequisite for the design and optimization of their production plants. They are widely used for industrial and residential purposes. [1-5]. Therefore, accurate knowledge of thermophysical properties of polymeric materials is valuable as it is required to decide whether the use of these fluids could be extended from the laboratory level to large-scale industrial applications. Although some experimental data exist, prediction of thermophysical properties of polymers such

as density and isothermal compressibility is still an important task considering they have been in focus as materials offering many highly promising applications. Under this circumstance, the development of equation of state (EOS) methods for the prediction of volumetric and thermodynamic properties of molten polymers can be highly useful.

Several researchers have previously applied the analytical EOSs to describe volumetric properties of molten polymers. For example, Sabzi-Boushehri (S & B) [6] have utilized the original version of Ihm-Song-Mason (ISM) EOS [7] for 4 polymer melts by means of surface tension and the molar density, both at the freezing point for the determination

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of ISM EOS parameters. Recently, Yousefi [8] has employed Tao-Mason (TM) EOS [9] for the estimation of volumetric properties of 8 molten polymers. She determined three temperature-dependent parameters of TM EOS by the help of temperature and liquid density (ρ_g) at the glass transition (T_g), as scaling constants. She has predicted 804 data points for the specific volumes with AAD equal to 0.34%. Yousefi et al. [10] have also applied the above mentioned scaling constants, i.e., temperature and density at glass transition point to ISM EOS for predicting the volumetric properties of 9 polymeric systems. They have predicted 1079 data points for the specific volumes with AAD equal to 0.40%. However, the need for surface tension and liquid density data both at freezing point and glass transition point, respectively, limits the applicability of the above-cited works because these values are not easily available for most polymers.

In this study, we demonstrate that there is no need for freezing and glass transition data to evaluate three temperature-dependent parameters of ISM EOS. To other word, these parameters will be determined based on the alternative (molecular) scaling constants contrary to the preceding works of Yousefi et al. [8,10], where the required scaling constants were taken from the bulk properties, e.g., liquid density at glass transition point.

Moreover, another distinctive feature of this work is applying the fixed free parameters, λ to ISM EOS [7]. This significance making it possible to reduce the number of input constants to be used in the EOS with respect to the previous works of Yousefi et al. [8,10], in which further inputs are required for each polymer by considering the temperature dependence of λ .

In this paper, the performance of the ISM based on the proposed molecular scaling constants has also been checked by predicting the estimation of isothermal compressibility

coefficient of molten polymers with reasonably good AAD which indicates the superiority of proposed method against the previous works of Yousefi et al [8,10] (i.e., AADs of the estimated κ_T were found to be more than 30%).

2. Theory

The general frame of the ISM EOS [7] can be summarized as:

$$\frac{P}{\rho k_B T} = 1 + \frac{(B_2(T) - \alpha(T) \rho)}{1 + 0.2 \lambda b(T) \rho} + \frac{\alpha(T) \rho}{1 - \lambda b(T) \rho} \quad (1)$$

where P is the pressure, ρ is the molar (number) density, $B_2(T)$ is the second virial coefficient, $\alpha(T)$ is the contribution of repulsive branch of pair potential function according to Weeks-Chandler-Anderson approach in perturbation theory of liquids [11]. This is based on the recognition that the structure of a liquid is determined primarily by repulsive forces, so that fluids of hard bodies can serve as useful reference states $b(T)$ reflects the van der Waals co-volume, $k_B T$ is the thermal energy per segment. λ is a free parameter which can be varied to get the desired volumetric data of dense fluids at the singular point.

The ISM equation of state requires the usage of the second virial coefficient, $B_2(T)$, along with the parameters $\alpha(T)$ and $b(T)$. For central force fields, the second virial coefficient is related to the intermolecular potential energy $u(r)$ through the following equation:

$$B_2(T) = 2\pi N_A \int_0^\infty (1 - e^{-u(r)/k_B T}) r^2 dr \quad (2)$$

Where N_A is the Avogadro's number.

If a two-parameter potential energy function $u(r)$ can describe the nature of the interaction potential between particles of a fluid, the potential can be written in

dimensionless form by:

$$\frac{u}{\varepsilon} = F\left(\frac{r}{\sigma}\right) \quad (3)$$

where ε is a characteristic energy parameter and σ is a characteristic size parameter, and F is a universal function of the reduced intermolecular separation

This function, $B_2(T)$ can be determined either by a direct correlation of experimental data for the second virial coefficient or by specification of the universal potential function u/ε and integration. In this work, we have taken ε as the energy parameters and σ as the size parameter in the potential energy relation as molecular scaling constants. Because, it was empirically found that σ^3 and ε/k_B both are closely proportional to the reciprocal density and to the inter-molecular energy changes during the phase transitions, respectively.

In this section the temperature-dependant parameters $B_2(T)$, $\alpha(T)$ and $b(T)$ of Eq. (1) are to be evaluated. We have used the alternative scaling constants; i. e., dispersive energy parameter (ε) and segment size (σ) to express $B_2(T)$, $\alpha(T)$ and $b(T)$ in terms of the universal functions of reduced temperature ($T_r = k_B T/\varepsilon$) as the following equations:

$$B_2(T)(N_A \sigma^3) = F_2\left(\frac{k_B T}{\varepsilon}\right) \quad (4)$$

$$\alpha(T)(N_A \sigma^3) = F_\alpha\left(\frac{k_B T}{\varepsilon}\right) \quad (5)$$

and

$$b(T)(N_A \sigma^3) = F_b\left(\frac{k_B T}{\varepsilon}\right) \quad (6)$$

It should be mentioned that the above mentioned temperature-dependent parameters, $B_2(T)$, $\alpha(T)$ and $b(T)$ reflect a measure of pairwise interactions.

3. Results and discussion

3.1. PVT properties

To utilize the proposed EOS two pure-component parameters of molten polymers must be characterized. Table 1 has been presented to provide the required pure-component parameters (σ , ε/k_B) for studied systems as well as their monomer molecular weight and glass transition temperature, T_g .

At first, we examined the accuracy of ISM EOS for the prediction of the specific volume of studied molten polymers. For this purpose, the specific data of 4 molten polymers have been taken, for which their measured values were available in the literature [15]. The results for 4 studied polymers were reported in Tables 2-5 as the relative deviations (RD in %) of the predicted specific volumes from the literature data [15]. To show the accuracy of the present work, the maximum deviations (in %) of the predicted specific volumes have also been indicated by bold faces in Tables 2-5.

Table 1. Optimized pure-component parameters of the ISM EOS for studied molten polymers

Polymer	MMW ^a (g/mol)	ε/k_B (K)	σ (nm)	λ	T_g ^b (k)
PO	112	461.05	0.6135	0.5148	338
PVME	58.00	440.19	0.38299	0.8908	239
PVC	62.50	422.16	0.36499	0.8158	358
PS	104.0	517.86	0.50799	0.6898	373

^a MMW is the monomer molecular weight.

^b these values were taken from Refs. 12-14.

Table 2. Relative deviation (in %)^a of the predicted specific volumes of PS using the proposed EOS at several isotherms, compared with the literature data [15]

P/ MPa	391.45 K	413.75 K	435.55 K	455.75 K	478.55 K	501.05 K	534.95 K	556.25 K	557.25K
0.1	-1.88	-1.73	-1.51	-1.16	-0.62	0.05	1.32	2.26^b	1.38
10	-1.66	-1.54	-1.34	-1.05	-0.60	-0.03	1.02	1.76	0.94
20	-1.45	-1.36	-1.19	-0.95	-0.55	-0.06	0.80	1.41	0.65
30	-1.25	-1.18	-1.06	-0.85	-0.52	-0.11	0.61	1.10	0.39
40	-1.06	-1.01	-0.92	-0.76	-0.48	-0.13	0.47	0.88	0.20
50	-0.89	-0.85	-0.80	-0.67	-0.44	-0.15	0.34	0.68	0.02
60	-0.75	-0.71	-0.67	-0.58	-0.39	-0.14	0.26	0.54	-0.09
70	-0.62	-0.57	-0.56	-0.50	-0.35	-0.15	0.19	0.42	-0.19
80	-0.52	-0.43	-0.45	-0.41	-0.29	-0.14	0.13	0.31	-0.28
90	-0.41	-0.29	-0.33	-0.33	-0.25	-0.11	0.09	0.24	-0.34
100	-0.32	-0.17	-0.23	-0.24	-0.19	-0.09	0.06	0.18	-0.39
110	-0.24	-0.04	-0.12	-0.16	-0.14	-0.07	0.05	0.12	-0.42
120	-0.15	0.07	-0.02	-0.08	-0.08	-0.04	0.02	0.08	-0.45
130	-0.07	0.17	0.08	0.00	-0.02	0.00	0.03	0.06	-0.51
140	0.01	0.27	0.19	0.09	0.03	0.03	0.03	0.03	-0.48
150	0.08	0.35	0.29	0.17	0.10	0.07	0.04	0.02	-0.47
160	0.15	0.44	0.38	0.25	0.17	0.12	0.06	0.02	-0.46
170	0.23	0.52	0.48	0.34	0.24	0.17	0.09	0.03	-0.45
180	0.30	0.59	0.58	0.42	0.31	0.23	0.11	0.04	-0.43
190	0.37	0.67	0.68	0.52	0.38	0.28	0.14	0.07	-0.40
200	0.44	0.73	0.77	0.59	0.45	0.35	0.19	0.09	-0.38

Table 3. Relative deviation (in %)^a of the predicted specific volumes of PVME using the proposed EOS at several isotherms, compared with the literature data [15].

P/ MPa	311.5K	340.3K	353.5K	374.5K	394.5K	415.5K
0.1	-1.93^b	-1.87	-1.60	-1.01	-0.39	0.41
5	-1.80	-1.73	-1.48	-0.90	-0.32	0.43
10	-1.67	-1.59	-1.35	-0.80	-0.25	0.44
20	-1.42	-1.35	-1.12	-0.60	-0.13	0.50
30	-1.18	-1.10	-0.92	-0.44	-0.02	0.51
40	-0.95	-0.89	-0.73	-0.27	0.11	0.58
50	-0.72	-0.67	-0.54	-0.12	0.22	0.63
60	-0.51	-0.48	-0.37	0.02	0.32	0.66
70	-0.31	-0.29	-0.20	0.16	0.41	0.72
80	-0.10	-0.12	-0.05	0.29	0.51	0.77
90	0.07	0.05	0.10	0.41	0.60	0.81
100	0.25	0.21	0.24	0.53	0.70	0.86
110	0.42	0.37	0.37	0.64	0.77	0.91
120	0.58	0.52	0.49	0.75	0.86	0.96

$$^a RD = \left(\frac{V^{Calc.} - V^{Exp.}}{V^{Exp.}} \right) \cdot 100$$

^b Bold face is the maximum %RD in the predicted specific volumes.

Table 4. Relative deviation (in %) ^a of the predicted specific volumes of PVC using the proposed EOS at several isotherms, compared with the literature data [15].

P/MPa	373.15K	383.25K	393.25K	403.25K	413.25K	423.15K
0	-0.18	-0.04	0.15	0.41	0.74	1.14^b
10	-0.20	-0.08	0.08	0.31	0.58	0.84
20	-0.20	-0.11	0.03	0.22	0.46	0.75
30	-0.20	-0.13	-0.02	0.15	0.36	0.61
40	-0.21	-0.14	-0.04	0.10	0.27	0.49
50		-0.15	-0.06	0.05	0.21	0.38
60		-0.15	-0.08	0.02	0.15	0.31
70		-0.15	-0.09	-0.01	0.12	0.24
80		-0.15	-0.10	-0.03	0.06	0.19
90			-0.11	-0.04	0.05	0.14
100			-0.11	-0.05	0.02	0.29
110			-0.10	-0.06	0.01	0.08
120			-0.10	-0.07	-0.01	0.06
130				-0.06	-0.02	0.04
140				-0.05	-0.03	0.03
150				-0.04	-0.02	0.02
160				-0.05	-0.02	0.02
170				-0.03	-0.02	0.01
180					-0.01	0.02
190					0.01	0.02
200					0.01	0.02

Table 5. Relative deviation (in %) ^a of the predicted specific volumes of PO using the proposed EOS at several isotherms, compared with the literature data [15]

P/MPa	455.9K	465.85K	476.1K	485.95K	496.2K	505.75K	516.5K	526.15K	536.75K
0.1	-1.19	-0.89	-0.49	-0.20	0.27	0.71	1.25	1.75	2.41
10	-1.00	-0.75	-0.44	-0.18	0.19	0.49	0.92	1.29	1.78
20	-0.81	-0.62	-0.35	-0.11	0.14	0.36	0.72	1.01	1.38
30	-0.69	-0.53	-0.32	-0.12	0.09	0.27	0.49	0.72	1.02
40	-0.57	-0.47	-0.29	-0.13	0.04	0.16	0.37	0.51	0.75
50	-0.46	-0.39	-0.26	-0.16	-0.01	0.08	0.24	0.37	0.52
60	-0.36	-0.31	-0.22	-0.15	-0.03	0.03	0.14	0.23	0.36
70	-0.25	-0.23	-0.17	-0.15	-0.06	-0.02	0.06	0.12	0.21
80	-0.15	-0.16	-0.12	-0.12	-0.06	-0.07	0.01	0.04	0.10
90	-0.07	-0.09	-0.07	-0.10	-0.07	-0.08	-0.05	-0.03	0.01
100	0.03	-0.01	-0.01	-0.06	-0.04	-0.09	-0.07	-0.07	-0.05
110	0.14	0.06	0.04	-0.02	-0.02	-0.09	-0.08	-0.11	-0.11
120	0.25	0.15	0.11	0.02	0.01	-0.07	-0.07	-0.12	-0.13
130	0.34	0.24	0.19	0.09	0.04	-0.04	-0.06	-0.11	-0.15
140	0.44	0.34	0.26	0.15	0.10	-0.01	-0.04	-0.11	-0.16
150	0.56	0.42	0.35	0.22	0.15	0.03	-0.02	-0.10	-0.15
160	0.66	0.53	0.45	0.29	0.20	0.07	0.03	-0.07	-0.13
170	0.76	0.64	0.53	0.36	0.26	0.12	0.06	-0.04	-0.10
180	0.87	0.73	0.61	0.45	0.33	0.17	0.11	0.00	-0.08
190	0.98	0.84	0.71	0.53	0.40	0.24	0.15	0.04	-0.04
200	1.07	0.94	0.79	0.62	0.47	0.30	0.22	0.09	-0.01

Generally, our calculation results over the whole pressure/temperature range were summarized as average absolute deviation percent (AAD in %) from literature data [15] in Table 6. As indicated by Table 6, from 547 data points examined for studied polymers in wide pressure range between 0.1 - 200 MPa and the temperature range from 311 to 557 K, AAD was found to be 0.47%. It should be mentioned that, the range of deviations in the current prediction was of the order of $\pm 2.86\%$.

Table 6 also compares our prediction results with those obtained from the preceding work of S & B [6] and Yousefi et al. [10], which employed ISM and TM EOSs, respectively, to predict specific volumes of molten polymers based on the scaling constants raised by the bulk properties contrary to the present work,

in which the alternative correlation equations based on the molecular scaling constants were presented. As Table 6 shows, our prediction results are almost as accurate as the previous works [6,10].

In order to illustrate how the ISM EOS passes through the experimental points, Figure 1 has been presented. It indicates the specific volume of PVC versus pressure at several isotherms. The markers represent the literature data [15] and the solid lines are those estimated from Eq. (1). As it is obvious from Figure 1, the agreement of the predicted values and literature data is quite good. The maximum RD is not more than 1.14%.

Moreover, it has been found that the predicted specific volumes have been affected by pressure, systematically, as it's impressed

Table 6. Average absolute deviation (AAD in %) of the predicted specific volumes of the molten polymers studied in this work, using the proposed EOS, compared with results from ISM and TM, all were compared with the literature data [15].

Polymer	ΔP (MPa)	ΔT (K)	NP ^a	this work	ISM [6]	TM [8]
PVME	0.1-120	311-415	84	0.88	0.30	0.26
PVC	0-200	373-423	85	0.15	0.14	0.21
PS	0.1-200	391-557	189	0.62	0.51	0.54
PO	0.1-200	456-536.7	189	0.31		
Overall			547	0.47	0.42	0.40

^a NP represents the number of data points examined

$$^b \text{AAD} = 100/\text{NP} \sum_{i=1}^{\text{NP}} |V_{i \text{ Cal.}} - V_{i \text{ Exp.}}| / V_{i \text{ Exp.}}$$

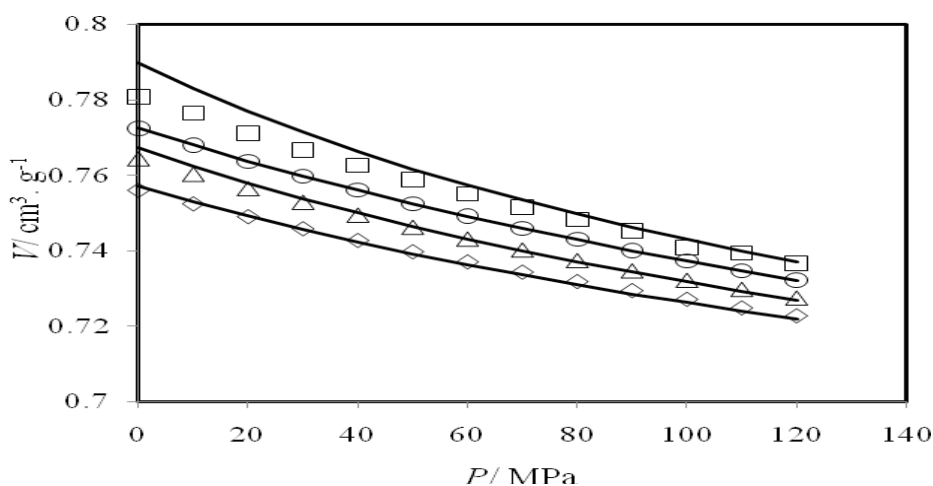


Fig. 1: The specific volume (V in $\text{cm}^3 \text{g}^{-1}$) of PVC versus pressure at several isotherms. The markers represent the experimental data [15] and the solid lines are those estimated from ISM EOS; 393.25 K (\diamond), 403.25 K (Δ), 413.25 K (\circ), and 423.25 K (\square).

from Tables 2-5. Since, the ISM EOS has been parameterized by some PVT data at moderate pressures; the high deviations have been appeared in the current predictions at low and high pressures accordingly.

3.2. First derivative thermodynamic properties

In this section, the relevant thermodynamic properties of molten polymer to the first derivation of ISM EOS were also predicted. Typically, the isothermal compressibility coefficient, κ_T is calculated using the isothermal pressure derivative of density/specific volume according to following equation:

$$\kappa_T = - \left(\frac{1}{V_S} \right) \left(\frac{\partial V_S}{\partial P} \right)_T = \frac{1}{\rho} \left(\frac{\partial \rho}{\partial P} \right)_T \quad (7)$$

We compared the calculated κ_T of PO using ISM EOS with those obtained from Tait equation [16]. The results were reported in Table 7 as the relative deviations (RD in %) of the predicted κ_T using ISM EOS from those derived by the Tait equation [16]. From 188 data points examined, the AAD of estimated κ_T was equal to 7.75%. According to Table 7, the maximum value of relative deviations (RD) for isothermal compressibility coefficients was found to be 24.38%. Generally, the reason

Table 7. Relative deviation (in %)^a of the predicted isothermal compressibility coefficients (κ_T) of PO using the proposed EOS at several isotherms, compared with the those obtained from the Tait equation [16].

P/ MPa	455.9K	465.85K	476.1K	485.95K	496K	505.7K	516K	526K	536.7K
0.1	-10.35	-6.25	-1.97	2.18	6.54	10.65	15.33	19.60	24.38
10	-10.00	-6.11	-2.11	1.73	5.70	9.36	13.46	17.12	21.11
20	-9.92	-6.23	-2.46	1.12	4.78	8.14	11.85	15.10	18.61
30	-10.04	-6.52	-2.95	0.41	3.84	6.95	10.36	13.34	16.51
40	-10.30	-6.94	-3.54	-0.36	2.87	5.79	8.97	11.73	14.65
50	-10.66	-7.43	-4.19	-1.17	1.89	4.64	7.64	10.22	12.96
60	-11.08	-7.99	-4.89	-2.00	0.91	3.52	6.36	8.80	11.37
70	-11.56	-8.58	-5.61	-2.84	-0.06	2.43	5.12	7.44	9.88
80	-12.08	-9.21	-6.34	-3.69	-1.03	1.36	3.93	6.14	8.47
90	-12.62	-9.85	-7.09	-4.53	-1.98	0.31	2.78	4.89	7.12
100	-13.18	-10.50	-7.84	-5.37	-2.91	-0.71	1.66	3.69	5.82
110	-13.75	-11.16	-8.58	-6.20	-3.83	-1.71	0.57	2.53	4.58
120	-14.33	-11.82	-9.32	-7.02	-4.73	-2.68	-0.48	1.41	3.39
130	-14.91	-12.47	-10.06	-7.83	-5.61	-3.63	-1.50	0.33	2.24
140	-15.49	-13.13	-10.78	-8.62	-6.47	-4.55	-2.49	-0.72	1.13
150	-16.08	-13.78	-11.50	-9.40	-7.31	-5.45	-3.45	-1.74	0.05
160	-16.66	-14.42	-12.20	-10.17	-8.13	-6.33	-4.38	-2.72	-0.99
170	-17.23	-15.05	-12.90	-10.91	-8.94	-7.18	-5.29	-3.68	-1.99
180	-17.80	-15.68	-13.58	-11.65	-9.73	-8.01	-6.18	-4.61	-2.96
190	-18.37	-16.30	-14.25	-12.37	-10.49	-8.83	-7.04	-5.51	-3.91
200	-18.92	-16.90	-14.91	-13.07	-11.24	-9.62	-7.87	-6.39	-4.83

$$^a R D = \left(\frac{\kappa_T^{Calc.} - \kappa_T^{Tait}}{\kappa_T^{Tait}} \right) \cdot 100$$

^b Bold face is the maximum %RD in the predicted κ_T .

for such high deviations is that κ_T is nearly related to isothermal EOS derivation against density/volume which resulted serious changes in the original frame of ISM EOS, by which the PVT data were predicted well. So, the large deviations related to the prediction of first derivative properties would be expectable.

Figure 2 depicts κ_T (in GPa^{-1} units) versus pressure for PO at several isotherms graphically. The solid lines are our predictions and the markers represent those obtained from the Tait equation [16].

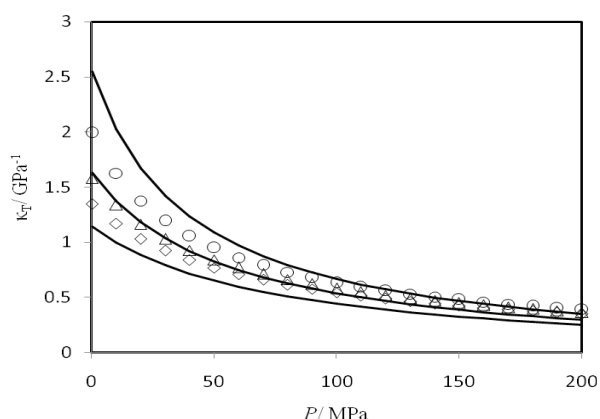


Fig.2: κ_T (in GPa^{-1} units) versus pressure for PO at several isotherms. The solid lines are our predictions and the markers represent those obtained from the Tait equation [13]. 456 K (\diamond), 486 K (Δ), and 526 K (\circ).

4. Conclusion

Finally, an analytical EOS has been employed to predict the volumetric and thermodynamic data of molten polymers. Knowing only two molecular scaling constants, ε/k_B and σ , is sufficient to determine the temperature-dependent parameters of the ISM EOS. Our calculations on the volumetric and thermodynamic properties of studied polymers reproduce the literature data over the whole liquid range with reasonably good accuracy.

Acknowledgment

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supports.

Nomenclature and units

List of symbols

AAD	average absolute deviation (%)
k_B	Boltzmann's constant (J K^{-1})
NP	number of data points
P	pressure (Pa)
T	Absolute temperature (K)
V	Specific molar volume ($\text{m}^3 \text{mol}^{-1}$)
MMW	monomer molecular weight (g. mol^{-1})
R	Universal gas constant ($\text{J mol}^{-1} \cdot \text{K}^{-1}$)
B_2	second virial coefficient/ (m^3)
b	co-volume/ (m^3)
a	repulsive contribution to pair potential function/ (m^3)
N_A	Avogadro's number

Greek letters

ρ	molar density (mol m^{-3})
σ	segment diameter (nm)
ε	dispersive energy parameter (J)
λ	free parameter

Superscripts

Calc	Calculated values
Exp	Experimental value

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Effect of Ionic Strength on Deprotonation of Salicylic Acid and its Derivative

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Abstract

The protonation constant values of salicylic and 5-nitrosalicylic acid were studied by a combination of spectrophotometric and potentiometric methods at 25 °C in wide range of ionic strength. The ionic strength of solutions was kept constant by sodium perchlorate as background electrolyte at 0.10 to 3.0 mol dm⁻³. Potentiometer was calibrated according to Gran method at each of ionic strength. The pK_a values were calculated using STAR program by multivariate curve fitting of absorbance data. The dependence of deprotonation constants on ionic strength were explained by means of Specific ion Interaction Theory (SIT). Activity coefficients of species were calculated by a modified SIT approach. The specific ion interaction parameters were extracted associated with the thermodynamic protonation constant.

Keywords: pK_a, Salicylic Acid, Ionic Strength, Specific ion Interaction Theory

1. Introduction

The acid dissociation or protonation constant, pK_a, plays an important role in physicochemical behavior of compounds in reaction media. It controls the extent of ionization of the molecules relative to the pH of solution. The determination of pK_a is essential in many different area such as chemistry, geology, biochemistry and medicine. For example, many of drugs have one or more acidic or basic functions in their structure which affect the membrane permeability and

solubility of those drugs [1]. In biochemistry, the protein stability and the activity of enzymes are closely related to protonation state of amino acid side chains [2]. In coordination chemistry, the extent of formation of complex is a function of protonation constant of ligands and pH of solution [3-7].

The equilibrium constants, such as protonation equilibrium, are usually determined in constant ionic strength by addition of an excess inert supporting electrolyte to solution to keep activity coefficient of all species constant during measurement process implementation. The equilibrium constants determined in this condition are named as the stoichiometric or conditional equilibrium

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constant. The knowledge of the activity coefficient of the species is needed to compare and predict conditional equilibrium constant in different ionic strength. A quantitative estimation of activity coefficient as a function of ionic strength in a broad range of electrolyte concentration can be provided by the Specific Ion Interaction Theory (SIT) [8]. This model has been successfully used in various studies for description of ionic strength effect on equilibrium constants and for determination of thermodynamics equilibrium constant by extrapolation to infinite dilution in which activity coefficient of species are unity [8-10].

Salicylic acid and some of its derivatives occur naturally in many fruits, plants and vegetables. They are the basic ingredient of a class of non-steroidal anti-inflammatory drugs with anti-pyretic, analgesic and anti-inflammatory effects [11]. The protonation constants of salicylic and 5-nitrosalicylic acid have been determined by some groups in different conditions and by a variety of methods [12-18]. However, to best of our knowledge, no systematic investigation has been done on ionic strength dependence of their protonation constants. In this study the protonation constants of salicylic and 5-nitrosalicylic acid have been determined in wide range of NaClO_4 electrolyte concentration. The dependence of protonation constants on ionic strength was studied by the SIT model. The thermodynamics protonation constants were calculated in infinite dilution together with the SIT interaction parameters.

2. Material and Methods

Salicylic acid and its 5-nitro derivative were supplied from Sigma-Aldrich. Sodium perchlorate as analytical reagent grade and titrasol solutions of NaOH and HCl were obtained of Merck. Water was double-distilled with conductivity of $1.3 \pm 0.1 \mu\Omega^{-1} \text{cm}^{-1}$.

A Jenway potentiometer, model 3520,

was used for potentiometric measurements. The *emf* of titration cell was measured by a combined glass electrode. A UV-Vis Shimadzu spectral photometer, model 2100, was used for spectrophotometric measurements. A double-walled reaction vessel was used as measurement cell with temperature thermostated at 25 °C. Constant ionic strengths of 0.1, 0.5, 1.0, 1.5, 2.0 and 3.0 mol dm^{-3} were maintained by concentrated solution of NaClO_4 . To avoid CO_2 contamination, a stream of purified nitrogen gas was bubbled through the solution during titration process.

In order to obtain exact concentration of H^+ during spectrophotometric titration, the potentiometric cell was calibrated according to Nernst's equation at each constant ionic strength. Solution of HCl with exact concentration was titrated by standardized NaOH solution. The formal electrode potential, E°_{cell} , and Nernst slope were computed in terms of known concentration of hydrogen ion for solutions at fixed ionic strength. For spectrophotometric titration, 25 mL of solution of salicylic and 5-nitrosalicylic acid was acidified to pH 2.0 and then titrated by stepwise addition of sodium hydroxide solution of 0.1 mol dm^{-3} . After each electrode stabilization, the *emf* and absorption spectra of solution were recorded in the interval of 200-400 nm. Then absorption data as a function of sample concentration and pH were introduced to STAR program to calculate the $\text{p}K_a$ values [19].

3. Results and Discussion

Calibration of potentiometric cell in each ionic strength

Glass electrode responses to activity of hydrogen ion rather than its concentration. However, the value of hydrogen ion concentration is needed for calculation of concentration quotients such as protonation constant. Therefore, prior to each

spectrophotometric titration, potentiometric cell is needed to be calibrated in terms of H^+ concentration [20]. The response of glass electrode theoretically follows the Nernst equation as [20-22].

$$E_{\text{cell}} = E_{\text{cell}}^{\circ} + k \log [H^+] + k \log \gamma_{H^+} + E_{\text{LJ}} \quad (1)$$

where E_{LJ} and k is the liquid junction potential and Nernst slope respectively. In theory, k is equal to $2.303RT/F$ with usual meaning for R, T and F . The formal electrode potential and the activity coefficient of hydrogen ion are represented by E_{cell}° and γ_{H^+} respectively. In constant ionic strength, parameters of E_{LJ} and γ_{H^+} are approximately constant and can be safely introduced into k_a . Therefore, equation 1 reduces to equation 2.

$$E_{\text{cell}} = k_a + k \log [H^+] \quad (2)$$

where k_a is equal to $E_{\text{cell}}^{\circ} + k \log \gamma_{H^+} + E_{\text{LJ}}$. The exact concentration of hydrogen ion is given by

$$[H^+] = (M_{\text{HCl}} V_0 - M_{\text{NaOH}} V_1) / (V_0 + V_1) \quad (3)$$

where M_i represents the molarities of i , V_0 and V_1 denote the initial volume of acid and the added volume of base solution, respectively. Calibration parameters including k_a and k were calculated from measured *emf* data using equations of 2 and 3. The experimental *emf* values are depicted as a function of negative logarithm of proton concentration in each ionic strength in figure 1.

In all experiments, the value of k were close to Nernst slope (theoretically equals to 59.167 mV at 25 °C) with correlation coefficients of approximately $r^2 = 0.99$. By having calibration parameters, the negative logarithm of concentration of hydrogen ion, p_cH , can be properly obtained by equation 4.

$$p_cH = (k_a - E_{\text{cell}}) / k \quad (4)$$

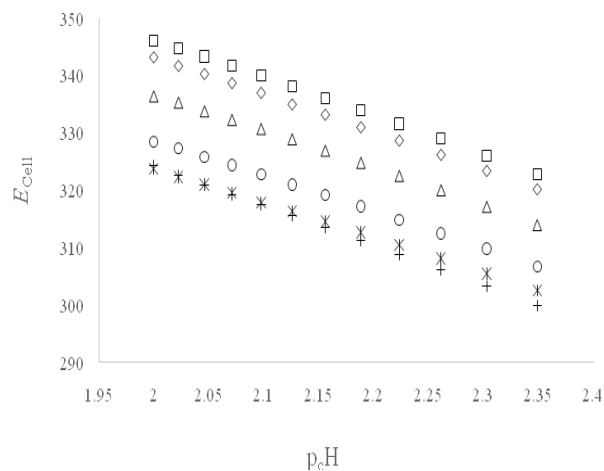


Fig. 1. Experimental *emf* values versus p_cH in ionic strength of 0.10 (+), 0.50 (*), 1.00 (O), 1.50 (Δ), 2.00 (\diamond) and 3.00 (\square) mol dm^{-3} NaClO_4

Calculation of protonation constants

Spectral change of 5-nitrosalicylic acid is shown typically at varying p_cH values in figure 2. Protonation constants were calculated by spectral data analysis in STAR program [19].

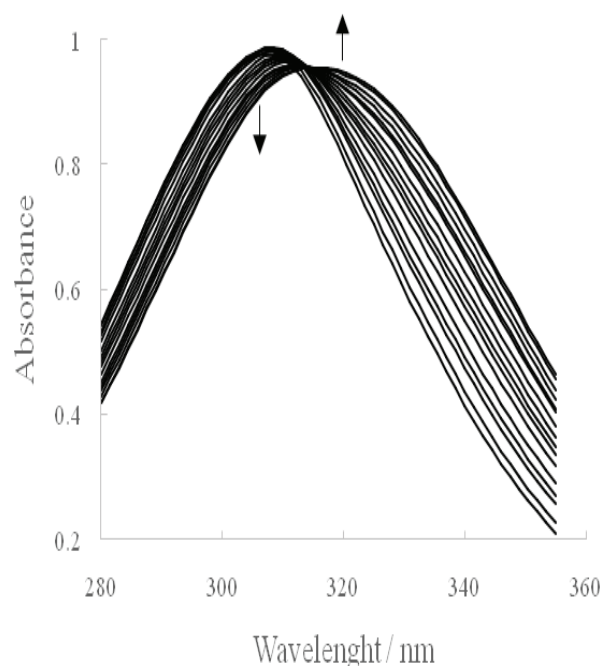


Fig. 2. Spectral change of 5-nitrosalicylic acid with increasing p_cH in ionic strength of 0.10 mol dm^{-3} NaClO_4

For each spectrophotometric titration, recorded spectra were arranged into a matrix R with dimension of $m \times n$. In matrix R , m is the number of spectra with different p_cH , and n is

the number of wave length in each spectrum at which the absorbance is recorded. According to Beer's law, matrix R can be represented by the matrix equation of 5

$$R = CS + E \quad (5)$$

Where $C(m \times p)$, $S(p \times n)$ and E are matrix of pure concentration, pure spectral profiles and optimal residual error respectively. Here p donates the number of absorbing species in the solution. The number of absorbing species was determined from factor analysis[19]. Rank analysis was performed by introducing M as $(1/n)RR^t$, where R^t is transpose of R . The rank of M , r_M , is mathematically equal to the number of eigenvectors with corresponding none zero eigenvalues. However, because of experimental error, the number of absorbing species is equal or lower than r_M . To this problem, in factor analysis, the standard deviation of the absorbance, SD, was calculated as a function of the number of none zero eigenvalues.

$$SD = \sqrt{\frac{\text{tr}(M) - \sum_{i=1}^j a_i}{m - j}} \quad (6)$$

Where $\text{tr}(M)$ and a_i are the trace and eigenvalue of component i of M matrix. Our results indicate that the spectral change observed during titration is attributed to two absorbing species, and therefore to the first deprotonation of compounds. By this knowledge, equation 5 was solved using hard modeling multivariate curve fitting. By initial estimation of protonation constant, fitting starts by calculation of the concentration profile of two absorbing species, matrix C , based on the mass action law constraint in terms of known total concentration and p_cH values during titration. At the same time, matrix S is solved under non-negative absorptivity

constraint for two absorbing species. In the nonlinear least-squares fitting, iterative cycles go on until to find the best set of parameters (protonation constant and molar absorptivities of species) that result in a minimum of E . Typically optimized concentration profile and pure spectra for two absorbing species of 5-nitrosalicylic acid is shown in figure 3.

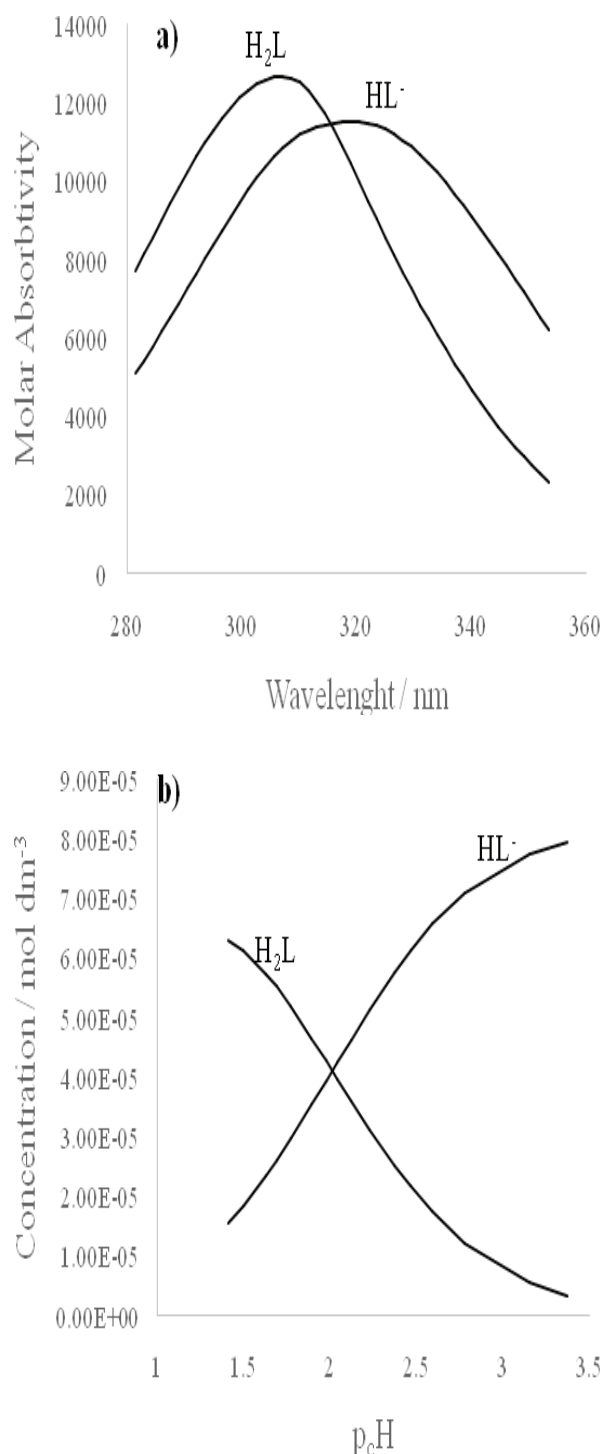


Fig. 3. a) Pure spectra and
b) Optimized concentration profile for 5-nitrosalicylic acid in ionic strength of $0.10 \text{ mol dm}^{-3} \text{ NaClO}_4$

Table 1. Protonation constants of salicylic acid and 5-nitrosalicylic acid at 25 °C and in different ionic strength of NaClO₄

I		pK _a ^{Salicylic Acid}		pK _a ^{5-nitrosalicylic Acid}		Reference
mol dm ⁻³	mol kg ⁻¹	mol dm ⁻³	mol kg ⁻¹	mol dm ⁻³	mol kg ⁻¹	
0.10	0.10	2.92 ± 0.01	2.91	2.02 ± 0.01	2.02	This work
0.50	0.51	2.72 ± 0.02	2.71	1.90 ± 0.01	1.89	-
1.00	1.05	2.83 ± 0.01	2.81	1.86 ± 0.02	1.84	-
1.50	1.62	2.84 ± 0.01	2.81	1.99 ± 0.01	1.96	-
2.00	2.21	3.01 ± 0.01	2.97	2.17 ± 0.01	2.13	-
3.00	3.50	3.18 ± 0.03	3.12	2.39 ± 0.02	2.32	-
0.20	-	2.75	-	-	-	[12]
0.10	-	2.90	-	-	-	[13]
0	-	2.97	-	-	-	[14]
0	-	3.02	-	-	-	[15]
0.10	-	2.81	-	2.20	-	[16]
0.10	-	2.77	-	1.92	-	[17]
0.10	-	2.83	-	-	-	[18]

The protonation constants determined by STAR program in different ionic strength are listed in Table 1 together with literature values. A disagreement between the values, obtained at the same ionic strength, may be attributed to the difference in experimental conditions involving the type of ionic media and the instrumental techniques.

Results indicate that the pK_a value of 5-nitro is lower than salicylic acid. It may be due to electron withdrawing effect of nitro group which makes deprotonated species more stable. Upon first deprotonation, molecules of salicylic acid and 5-nitrosalicylic acid take negative charge on their carboxylic group. However, the presence of electron withdrawing group of nitro on the structure of 5-nitro, results in inductive effect which stabilizes negative carboxylic group more effective than salicylic acid.

Ionic Strength Effect

As shown in Table 1, at first, the pK_a values of salicylic acid and 5-nitrosalicylic acid decreases with increasing ionic strength to 0.5 mol dm⁻³ and then increases with further increasing of ionic strength. This behavior is attributed to change of activity coefficient

of species with increasing of ionic strength. Activity coefficient of species are influenced by the type of interactions between ions. At low ionic strength, interactions between ions are of attractive type; resulting in activity coefficient lower than unity. However, as the ionic strength increases, the ionic atmosphere becomes more compressed and screens the ionic charges more effectively, so repulsive interactions become more important; resulting in activity coefficient higher than unity.

The deprotonation equilibrium of two hydroxybenzoic acids can be represented by equation 7.



According to equation 7, the deprotonation constant can be given by

$$K_a^T = \frac{[\text{H}^+][\text{HA}^-]}{[\text{H}_2\text{A}]} \frac{\gamma_{\text{H}^+}\gamma_{\text{HA}^-}}{\gamma_{\text{H}_2\text{A}}} = K_a \frac{\gamma_{\text{H}^+}\gamma_{\text{HA}^-}}{\gamma_{\text{H}_2\text{A}}} \quad (8)$$

Where γ_i is activity coefficient of species i ; represent thermodynamic deprotonation constant, and K_a stands for stoichiometric constant determined at each ionic strength. By

taking negative logarithm on equation 8

$$pK_a = pK_a^T + \log \gamma_{H^+} + \log \gamma_{HA^-} - \log \gamma_{H_2A} \quad (9)$$

The dependence of pK_a values on ionic strength may be analyzed by considering well known Specific Ion Interaction Theory (SIT) [8-10]. In original SIT model, activity coefficient of ion i with charge z_i can be expressed by equation 10 in the solution of ionic strength I (in molal scale) at 25 °C.

$$\log \gamma_i = -z_i^2 \frac{0.51\sqrt{I}}{1+1.5\sqrt{I}} + \sum_j \varepsilon_{ij} m_j \quad (10)$$

The ion interaction coefficient ε_{ij} , usually called SIT parameter, interprets the specific short range interactions of ion i with ion j in its molal concentration m_j . SIT model assumes that interaction coefficient is zero for two electrically like sign ions or neutral species.

By considering the SIT model for calculation of activity coefficients of species, equation 8 can be reformulated as following

$$pK_a = pK_a^T - z^* \frac{0.51\sqrt{I}}{1+\sqrt{I}} + \Delta\varepsilon I \quad (11)$$

Where

$$z^* = \sum (\text{charges})_{\text{products}}^2 - \sum (\text{charges})_{\text{reactants}}^2 \quad (12)$$

$$\Delta\varepsilon = \varepsilon_{HL^-, Na^+} + \varepsilon_{H^+, ClO_4^-} \quad (13)$$

It should be noted that pK_a and I values are in molal concentration scale.

Experimental pK_a values from Table 1 were fitted into equation 11 as a function of ionic strength by least squares regression analysis. The following expressions were obtained in accordance with SIT model where equations 14 and 15 are obtained for salicylic acid and 5-nitrosalicylic acid respectively.

$$pK_a = (3.04 \pm 0.04) - 2 \frac{0.51\sqrt{I}}{1+\sqrt{I}} + (0.16 \pm 0.02)I \quad (14)$$

$$pK_a = (2.14 \pm 0.04) - 2 \frac{0.51\sqrt{I}}{1+\sqrt{I}} + (0.19 \pm 0.02)I \quad (15)$$

The goodness of fit of SIT model was judged by excellent square correlation coefficients (r^2 is 0.936 and 0.939 for equation 14 and 15 respectively), associated with low values of standard deviation obtained for each of regression coefficients. The specific interaction coefficient of $HClO_4$ is 0.146 [23], therefore according to equation 13, the specific interaction coefficient between HA^- and Na^+ are calculated to be 0.014 and 0.044 for salicylic acid and 5-nitrosalicylic acid respectively.

4. Conclusion

The protonation constant of salicylic acid and 5-nitrosalicylic acid were investigated by an accurate spectroscopic method in wide range of ionic strength supplied by sodium perchlorate at 25 °C. The pK_a values assigned for first deprotonation equilibrium were calculated by multivariate curve fitting implemented in STAR program. Results show that in a regular trend, at first the pK_a decreases to a minimum value at around 0.5 mol kg⁻¹ of ionic strength; then increases with a relatively linear manner along the curve. The SIT theory was applied successfully to describe the ionic strength dependency of pK_a values. The thermodynamic deprotonation constant of salicylic acid and 5-nitrosalicylic acid were calculated as 3.04 and 2.14 respectively. Also the specific interaction coefficient between deprotonated form of salicylic acid and 5-nitrosalicylic acid with Na^+ are calculated as 0.014 and 0.044 respectively. The SIT models obtained can be used for estimation of protonation constants of salicylic acid and

5-nitrosalicylic acid in each ionic strength in the range of 0.0 to 3.0 mol dm⁻³ of NaClO₄.

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Equilibrium Modeling and Kinetic Studies on the Adsorption of Basic Dye by a Low Cost Adsorbent

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Abstract

An agricultural waste and eco-friendly biosorbent i.e. rice husk has been used as a cheap adsorbent for the removal of methylene blue dye from aqueous solutions. The physical properties of the developed adsorbent were characterized using FTIR. The study was realized using batch experiments. The effects of contact time, pH, initial dye concentration, biosorbent dose and temperature were investigated. The adsorption data were evaluated by Freundlich and Langmuir isotherm models. The adsorption isotherm is best fitted by the Freundlich model, while the adsorption kinetics is well described by the pseudo-second-order model. Different thermodynamic parameters i.e., changes in standard free energy, enthalpy and entropy have also been evaluated and it has been found that the dye adsorption onto rice was a spontaneous, endothermic and physical reaction.

Keywords: Rice husk; Biosorption; Kinetic study; Isotherm; methylene blue; basic dye

1. Introduction

Color is a visible pollutant and the presence of even a very minute amount of coloring substance makes it undesirable due to its appearance. The removal of color from dye-bearing effluents is a major problem due to the difficulty in treating such waste waters by conventional treatment methods. The sorption technique is proved to be an effective and attractive process for the treatment of these dye-bearing wastewaters [1,2]. The most widely used and effective physical method in industry is activated carbon, although running

costs are expensive [3]. If the adsorbent material used is of cheaper cost and does not require any expensive additional pretreatment step, this method will become inexpensive. In recent years, some papers had reported several kinds of agricultural by-product such as rice husk [4-5], cereal chaff [6], giant duckweed [7], sawdust [8] for the removal of methylene blue from its aqueous solutions.

Physical and chemical methods such as biological oxidation, adsorption, foam flotation, electrolysis, coagulation-flocculation, ozonation, oxidation, filtration, membrane separation, photo catalysis and electrochemical methods have been used for waste water decolourisation [9-20].

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The adsorption process is one of the most efficient methods of reactive, acidic and direct dyes in neutral solutions removing pollutants from wastewater and provides an attractive alternative treatment, especially if the biosorbent is inexpensive and readily available [21].

The abundance and availability of agricultural by-products make them good sources of cheap raw materials for natural adsorbents. Rice husk, an agricultural waste, has been reported as a good adsorbent for many metals and basic dyes [22-23]. Rice husk consists of 32.2% cellulose, 21.4% hemicelluloses and 21.3% lignin [24-25]. The cellulose, hemicellulose and lignin form a very stable matrix structure. The inner surface of rice husk is smooth, and may contain wax and natural fats that provide good shelter for the grain. On the other hand, the presence of these impurities on the inner surface of rice husk also affects the adsorption properties of rice husk, both chemically and physically [26]. Scanning Electron Microscope (SEM) of rice husk showed the morphological features of outer epidermis raw rice husk, which is well organized in structure that resembles rolling hills [27].

In the purpose of this work, adsorption capacity of rice husk for the adsorption of methylene blue dye from aqueous solutions has been investigated and the obtained experimental data were analyzed using isotherm models namely, Langmuir and Freundlich. The effect of pH, adsorbent amount, contact time, biosorbent dose, temperature and initial dye concentration has been studied. Kinetic experiments have been also conducted to determine the rate of adsorption. Methylene blue is the most commonly used material for dyeing cotton, wood and silk. Methylene blue was chosen because of its known strong adsorption onto solids and it serves as a model compound for removing organic contaminants and colored bodies.

2. Materials and methods

All chemicals and reagents were of analytical grade. Basic dye used in this study was methylene blue (molecular formula: $C_{16}H_{18}N_3ClS$, $\lambda_{max} = 665\text{nm}$) purchased from Merck. The experimental solutions were obtained by diluting the stock solution in accurate proportions to different initial concentrations. The rice husk was obtained from a farm near Omidiyeh city, Khuzestan state, Iran. Rice husk was washed several times with water followed by filtration. The cleaned rice husk was oven dried completely at 70°C , then cooled and sieved to $50\mu\text{m}$ size, which was used without further treatment.

2.1. Batch adsorption studies

Adsorption experiments were carried out by adding a fixed amount of rice husk to a series of Erlenmeyer flasks filled with 25 mL diluted solutions. The Erlenmeyer flasks were shaken at 300 rpm for 6 hours at room temperature. After equilibration, 10 mL of the suspension was centrifuged in a stopped tube for 10 min at 3000 rpm and 4 mL of the dye solution was taken from the tube by a filtered syringe for measurement. The color of dye concentrations were measured with a PerkinElmer Lambda 25 UV/Vis Spectrometer using maximum absorbance wave length values (λ_{max}) for each dye. To determine the optimum conditions of the several parameters such as contact time, pH, initial dye concentration, biosorbent dose and temperature were studied for methylene blue dye. Using optimum conditions dye removal capacity, equilibrium values and kinetic studies were performed for methylene blue dye.

The amount of methylene blue adsorption at equilibrium, q_e (mg/g) was calculated from the following equation [28]:

$$q_e = \frac{(C_0 - C_e) \times V}{w} \quad (1)$$

Where C_0 and C_e (mg/L) are the initial and equilibrium liquid phase concentration of dye solutions, respectively, V (L) the volume of the solution and W (g) is the mass of adsorbent. Decolourisation of dyes sorbed by rice husk was calculated using the following equation [28]:

$$\text{Removal percentage} = \frac{C_0 - C_e}{C_0} \times 100 \quad (2)$$

3. Results and discussion

3.1. Characterization of the adsorbent

FTIR spectroscopy was used for the characterization of rice husk. The FTIR spectrum (Fig. 1) indicated a broad band at 3410.24 cm^{-1} representing the bonded -OH groups. The C-H stretching vibration around 2925.16 cm^{-1} indicates the presence of alkane functional group. The peaks around 1648.38 - 1740 cm^{-1} correspond to the C=O stretching that may be attributed to the hemicelluloses and lignin aromatic groups [29]. The peaks around 1514.67 cm^{-1} indicate the presence of C=C stretching vibrations of alkenes and aromatic functional groups. The peaks around 1425.63 cm^{-1} indicate the presence of CH_2

and CH_3 groups [30]. A peak at 1376.64 cm^{-1} band may be attributed to the aromatic CH and carboxyl-carbonate structures. The peaks in the 1254.50 - 1300 cm^{-1} correspond to vibration of C-O group in lactones.

The peaks around 1045.14 , 578.92 and 465.93 cm^{-1} , correspond to CHOH stretching, Si-O-Si stretching and Si-H groups, respectively. The presence of polar groups on the surface is likely to provide the considerable cation exchange capacity to the adsorbent [30].

3.2. Effect of different parameters

3.2.1. Effect of pH

The pH was adjusted using 0.1 N NaOH and 0.1 N HCl solutions. The pH of the dye solution plays an important role in the whole biosorption process and especially on the biosorption capacity. FTIR spectrum showed that rice husk has -OH groups. So, it seems that the pH value can affect the adsorbent efficiency of rice husk. The effect of pH of the solution on the adsorption efficiency of rice husk has been shown in Fig. 2. It can be seen from the figure that as the solution pH increases, the adsorption capacity increases.

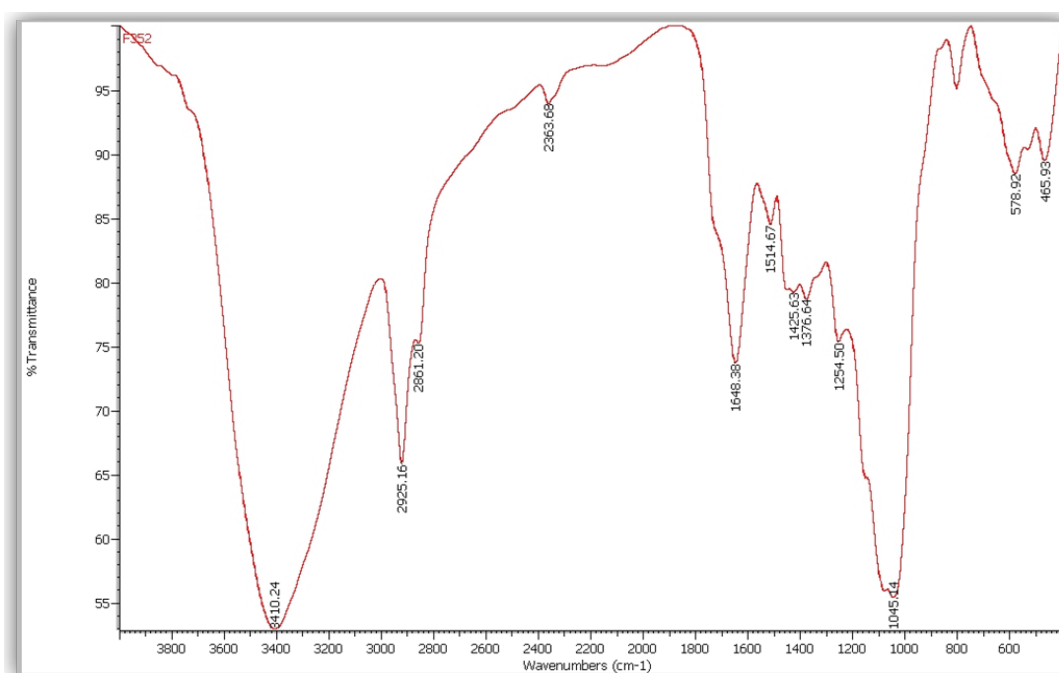


Fig.1. FTIR spectra of Rice husk.

Increasing solution pH increases the number of hydroxyl groups thus, increases the number of negatively charge sites and enlarges the attraction between dye and adsorbent surface [31]. Generally, the net positive charge decreases with increasing pH value lead in the decrease in the repulsion between the adsorbent surface and the dye thus, improving the adsorption capacity.

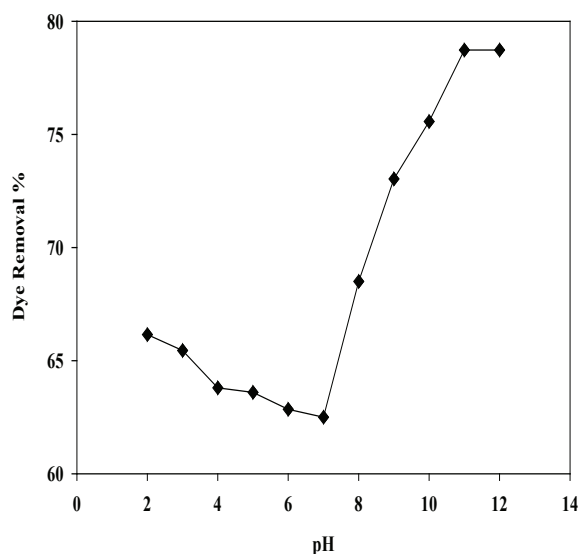


Fig. 2. Effect of pH on the removal of methylene blue by rice husk (Contact time 6 h, biosorbent dose 0.1 g, initial concentration of dye 12 mg/L and 30°C).

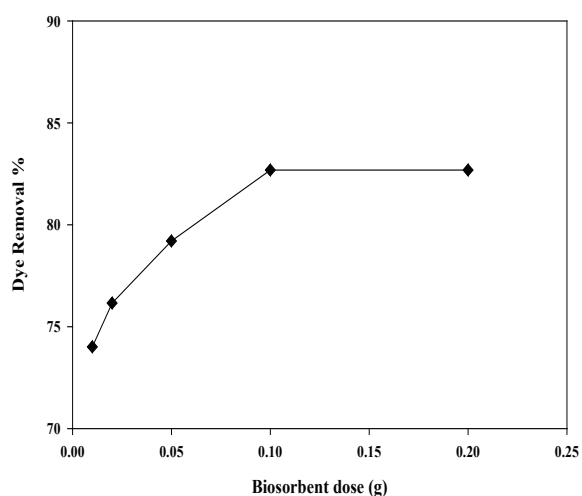


Fig. 3. Effect of biosorbent dose on the removal of methylene blue by rice husk (Contact time 6 h, pH 11, initial concentration of dye 12 mg/L and 30°C).

3.2.2. Effect of biosorbent dose

In order to evaluate the maximum biosorption capacity of the rice husk, the effect of biosorbent dose was investigated. The dose of respective biosorbent was varied from 0.01 to 0.2 g at a fixed pH, temperature and adsorbate concentration. After 0.1 g of the adsorbent, there was no change in the adsorption efficiency. So, 0.1 g of the adsorbent was chosen as an optimum amount. Results were shown in Fig. 3.

3.1.3. Effect of contact time

For the biosorption processes, biosorption experiments were carried out for different contact times with a fixed biosorbent dose 0.1 g, initial dye concentration 12 mg/L at solution pH 11 and at 30°C (Fig. 4). It is observed that the uptake of the dye increases with time. The uptake of adsorbate species was rapid in the initial stages of the contact period and became slow near the equilibrium. The percentage of dye removal at contact time of 60 min was 77.88%. After this time no further increase in the adsorption was observed. This result is expected because a large number of surface sites are available for adsorption at the initial stages and after a lapse of time, the remaining surface sites are difficult to occupy because of

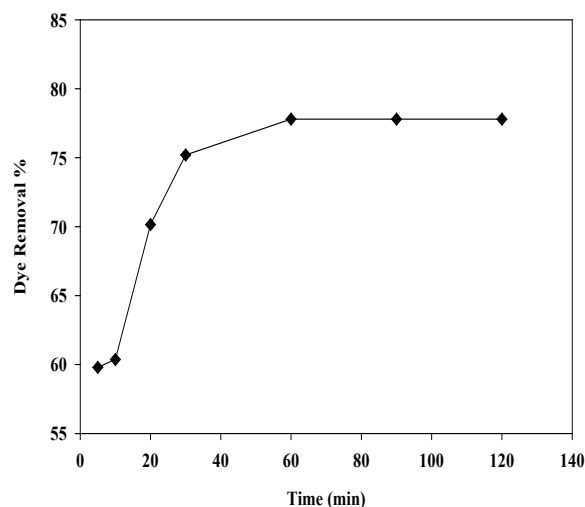


Fig. 4. Effect of contact time on the removal of methylene blue by rice husk (Biosorbent dose 0.1g, pH 11, initial concentration of dye 12 mg/L and 30°C).

repulsion between the solute molecules of the solid and bulk phases [32].

3.1.4. Effect of dye concentration

Different methylene blue dye concentrations (8-16 mg/L) were used to determine the effect of dye concentration. The increase in the dye concentration leads to a decrease in the percentage of methylene blue removal (Fig. 5). As the dye/ sorbent ratio increases, sorption sites are saturated, resulting in decreases in sorption efficiency [33].

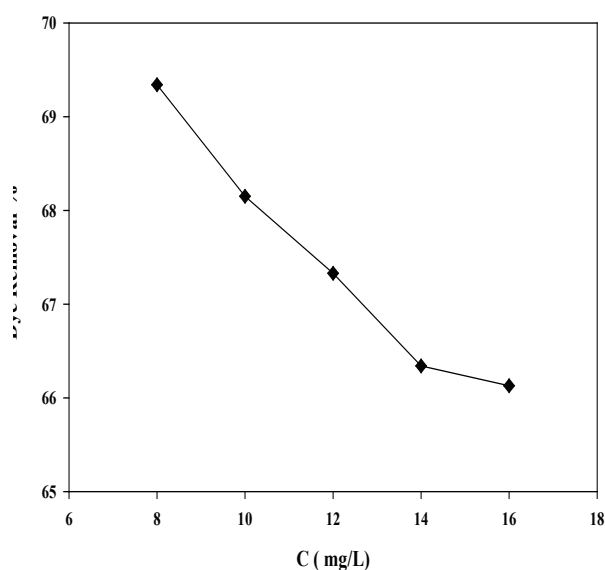


Fig.5. Effect of dye concentration on the removal of methylene blue by rice husk (Contact time 60 min, Biosorbent dose 0.1g, pH 11 and 30°C).

3.1.5. Effect of temperature

Biosorption experiments were carried out at different temperatures with a constant methylene blue concentration of 12 mg/L, biosorbent dose 0.1 g and pH 11. The removal percentage of methylene blue increases with increasing temperature, indicating that the sorption is **endothermic** process. This may be a result of increase in the mobility of dye with increasing temperature. Furthermore, the enhancement of sorption capacity might be due to the enhancement of sorptive interaction between the active site of rice husk and methylene blue or produce a swelling effect

within the internal structure of rice husk and enabling more dye molecules diffusion [34].

The thermodynamic parameters for the biosorption process, ΔH^0 , ΔS^0 and ΔG^0 , were evaluated using the equation [35,36]:

$$\Delta G^0 = -RT \ln K \quad (3)$$

$$\ln K = \frac{\Delta S^0}{R} - \frac{\Delta H^0}{RT} \quad (4)$$

$$G^0 = \Delta H^0 - T\Delta S^0 \quad (5)$$

Where K , known as the distribution coefficient of the adsorbate, is equal to (qe/Ce) . R is the gas constant ($8.314 \text{ J.mol}^{-1}.\text{K}^{-1}$) and T is the temperature in Kelvin. The plot of $\ln K$ vs. $1/T$ is linear with the slope and the intercept giving values of ΔH^0 and ΔS^0 , respectively (Fig. 6). These values could be used to compute ΔG^0 . All these relations are valid when the enthalpy change remains constant in the temperature range. These thermodynamic parameters are given in Table 1. Generally, the change of free energy for physical biosorption is smaller than that of chemical biosorption. The positive value of ΔH^0 shows that the

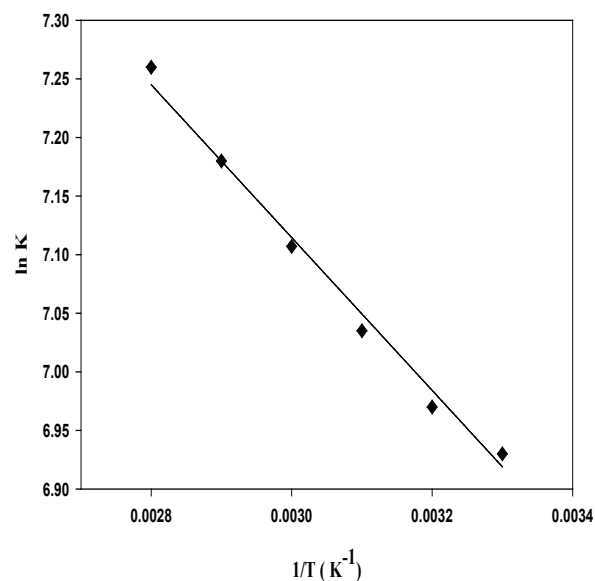


Fig. 6. Plot of $\ln K$ versus $1/T$ for estimation of the thermodynamic parameters.

adsorption is endothermic process while positive ΔS^0 value reflects the increasing randomness at the solid/solution interface during the adsorption. The change in free energy for physical and chemical reactions are between - 20 and 0 kJ.mol^{-1} and - 80 and - 400 kJ.mol^{-1} respectively [37].

3.3. Biosorption isotherms

The purpose of the adsorption isotherms is to relate the adsorbate concentration in the bulk and the adsorbed amount at the interface [38]. Biosorption isotherms are the most important information for analyzing and designing a biosorption process [39,40]. Several isotherm equations are available and two important isotherms are selected in this study, the Langmuir and Freundlich isotherms [41,42]. The Langmuir biosorption isotherm assumes that adsorption takes place at specific homogeneous sites within the biosorbent and has found successful applications for too many biosorption processes of monolayer adsorption.

The expression of the Langmuir model is given by Eq. (6) [43].

$$\frac{C_e}{q_e} = \frac{1}{q_m K_L} + \frac{C_e}{q_m} \quad (6)$$

Where q_e (mg/g) is the adsorbed amount of the dye, C_e (mg/L), is the equilibrium concentration of the dye in solution, q_m (mg/g) is the maximum adsorption capacity

and K_L (L/mg) is the energy of adsorption.

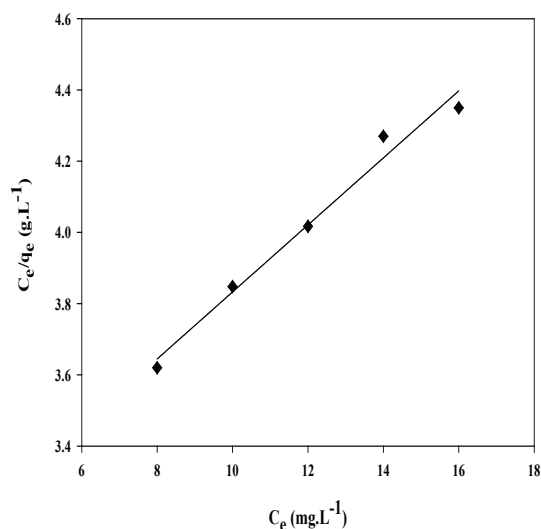


Fig. 7. Langmuir isotherm for methylene blue sorption onto rice husk (Contact time 60 min, Biosorbent dose 0.1g, pH 11 and 30°C).

Fig.7.shows a linear plot of C_e/q_e versus C_e . The Langmuir constants q_m and K_L were determined from the slope and intercept of the plot and are presented in Table 2. The important characteristic of the Langmuir isotherm can be expressed by means of dimensionless constant separation factor, which is calculated using the following equation:

$$R_L = \frac{1}{1 + K_L C_0} \quad (7)$$

Where K_L denotes the Langmuir constant and C_0 is the initial concentration [44]. At all initial concentrations within studied range, R_L values presented in Table 3 have been found between

Table 1: Thermodynamic parameters for biosorption of Methylene blue on rice husk at different temperatures

Temperature (K)	ΔG^0 (kJ.mol ⁻¹)	ΔH^0 (kJ.mol ⁻¹)	ΔS^0 (kJ.mol ⁻¹ K ⁻¹)
303	-14.02	3.46	0.057
313	-14.59		
323	-15.16		
333	-15.79		
343	-16.41		
353	-16.89		

0 and unity (1), indicating thereby favorable processes for the adsorbent. Also higher R_L values at lower dye concentrations show that the adsorption is more favorable at lower dye concentrations.

Table 2: Langmuir and Freundlich isotherm model constants and correlation coefficients for adsorption of methylene blue onto rice husk

Isotherm	Parameters
Langmuir	
q_m (mg.g ⁻¹)	13.63
K_L (L.mg ⁻¹)	0.038
R^2	0.981
Freundlich	
K_F	0.361
n	1.344
R^2	0.998

The Freundlich isotherm [45] is an empirical equation employed to describe heterogeneous systems. The Freundlich equation is expressed as:

$$q_e = K_F C_e^{1/n} \quad (8)$$

$$\ln q_e = \ln K_F + \frac{1}{n} \ln C_e \quad (9)$$

Where, K_F is biosorption capacity at unit concentration and $1/n$ is biosorption intensity. $1/n$ values indicate the type of isotherm to be irreversible ($1/n = 0$), favorable ($0 < 1/n < 1$) and unfavorable ($1/n > 1$). The biosorption capacity depends on the properties of adsorbate and biosorbent. To determine the constants K_F and n , the linear form of the equation may be used to produce a graph of $\ln(q_e)$ against $\ln(C_e)$ (Fig. 8) All constants obtained by Freundlich models are listed in Table 2. By comparing the results of the values, it was found that the Freundlich isotherm generally represent the equilibrium sorption of methylene blue onto rice husk.

Table 3: C_o and R_L values for adsorption of Methylene blue onto rice husk

C_o	R_L
8	0.615
10	0.561
12	0.516
14	0.478
16	0.444

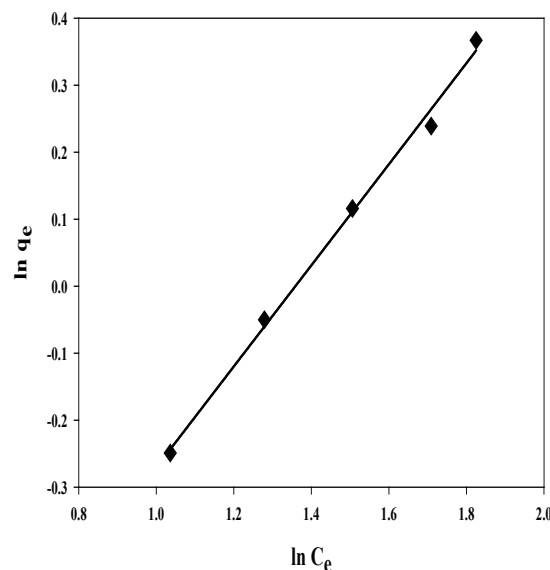


Fig. 8. Freundlich isotherm for methylene blue sorption onto rice husk (Contact time 60 min, Biosorbent dose 0.1g, pH 11 and 30°C).

3.4. Adsorption kinetics

A linear form of pseudo-first-order model was described by Lagergren [46] in the form:

$$\log(q_e - q_t) = \log q_e - \frac{K_1 t}{2.303} \quad (10)$$

A linear plot of $\log(q_e - q_t)$ against time allows one to obtain the rate constant (Fig. 9). If the plot was found to be linear with good correlation coefficient, indicating that Lagergren's equation is appropriate to methylene blue sorption on rice husk. So, the adsorption process is a pseudo-first-order process [46,47]. The Lagergren's first order rate constant (k_1) and q_e determined from the model are presented in Table 4 along with the corresponding correlation coefficients. It was

observed that the pseudo-first-order model did not fit well. It was found that the calculated q_e value does not agree with the experimental q_e value (Table 4). This suggests that the adsorption of methylene blue does not follow first-order kinetics.

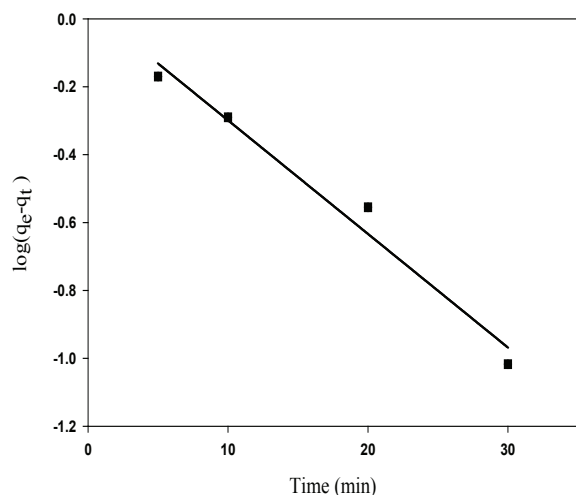


Fig. 9. Pseudo-first-order sorption kinetics for methylene blue sorption onto rice husk

The pseudo-second-order kinetics may be expressed in a linear form as [48,49]:

$$\frac{t}{q_t} = \frac{1}{k_2 q_e^2} + \frac{t}{q_e} \quad (11)$$

Where the equilibrium adsorption capacity (q_e), and the second order constant k_2 (g/mg min) can be determined experimentally from the slope and intercept of plot t/q_t versus t (Fig. 10). The k_2 and q_e determined from the model are presented in Table 4 along with the corresponding correlation coefficients.

The values of the calculated and experimental q_e are represented in Table 4. It can be seen that there is an agreement between q_e experimental and q_e calculated values for the pseudo-second-order model. Hence, the pseudo-second-order model better represented the adsorption kinetics. Similar phenomenon has been observed in the adsorption of methylene blue by hazelnut shells and wood sawdust [50].

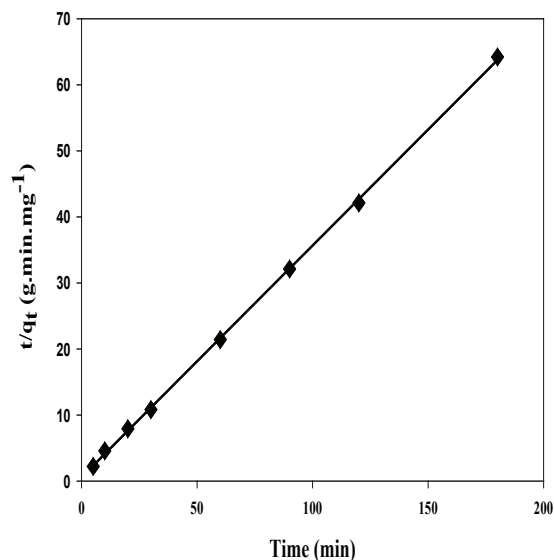
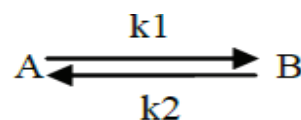


Fig. 10. Pseudo-second-order sorption kinetics for methylene blue sorption onto rice husk

Kinetics of sorption describes the solute uptake rate, which in turn governs the residence time or sorption reaction. It is one of the important characteristics in defining the efficiency of sorption. In this study, the kinetics of the methylene blue dye removal was carried out to understand the behavior of this low-cost adsorbent. The adsorption of methylene blue dye from an aqueous solution follows reversible second-order kinetics, when a single species is considered on a heterogeneous surface. The heterogeneous equilibrium between the methylene blue dye solution and the rice husk was represented in the following equation.



Where k_1 is the forward rate constant and k_2 is the backward rate constant. A represents the methylene blue remaining in the aqueous solution and B represents the methylene blue adsorbed on the surface of the rice husk. [51,24].

Another study of methylene blue onto rice husk showed that Equilibrium data fitted well into the Langmuir isotherm equation.

The sorption kinetics was found to follow a pseudo-second-order kinetic model [4]. A comparative case study of two models (Thomas model and bed-depth/service time analysis model) has shown that these models are suitable for describing the biosorption process of the dynamic behavior of removal methylene blue with the rice husk. All the results suggested that rice husk as adsorbent to removal methylene blue from solution be efficient, and the rate of biosorption process be rapid [5].

Table 4. Comparison of the pseudo-first-order, pseudo-second-order adsorption rate constants and calculated and experimental q_e values obtained at different initial methylene blue concentrations

Kinetic model	Parameters
Pseudo-first-order	
$q_{e,cal}$ (mg.g ⁻¹)	0.169
k_1 (min ⁻¹)	0.02
R^2	0.984
Pseudo-second-order	
k_2 (g. mg ⁻¹ .min ⁻¹)	0.474
$q_{e,cal}$ (mg.g ⁻¹)	1.135
h (mg.min ⁻¹ .g ⁻¹)	0.610
R^2	0.999
$q_{e,exp}$ (mg.g ⁻¹)	1.123

The value of q_m in the present work is compared with number of recently reported adsorbents used for the adsorption of methylene blue in Table 5. It is evident from Table 5 that the value of adsorption capacity in the present work (13.63 mg/g) is higher than some of adsorbents but lower than the activated carbon obtained from rice husk.

4. Conclusion

The present investigation showed that rice husk can be effectively used as adsorbent. The amount of dye sorbed was found to vary with initial solution pH, adsorbent dose, temperature and contact time. Methylene blue adsorption onto rice husk is increased with the rise in initial pH. The maximum monolayer adsorption capacity, q_{max} , at 25 °C of Methylene blue onto rice husk was found to be 13.63. The kinetics studies indicated that the adsorption kinetics of dye on rice husk followed the pseudo-second order. The equilibrium data have been analyzed. The results showed that the methylene blue followed Freundlich isotherm model. Thermodynamic studies indicated that the dye adsorption onto rice husk was a spontaneous, endothermic and physical reaction. Rice husk is economically

Table 5. Comparison of adsorption capacity of various adsorbents reported in literature and rice husk

Adsorbents	q_m (mg/g)	References
Rice husk (grinded to powder)	40.58	4
Neem leaf (powder)	8.76-1961	53
Eggshell and eggshell membrane	0.8-0.24	54
Fly ash	13.42	55
Wheat shells (grinded to powder)	16.56	56
Activated date pits (500°C)	12.9	57
Activated date pits (900°C)	17.3	57
Banana peel (washed and dried)	20.8	58
Pumpkin seed hull (crushed)	141.29	59
Rice Husk (washed and dried)	4.41	60
Rice Husk's activated carbon	441.52	61
Present work	13.63	

cheap and so regeneration is not necessary. Furthermore, being an agriculture waste, the rice husk is easily available and a cheap material in agricultural countries such as Iran, so it can be used as potential adsorbent for the removal of MB. Given the facts that rice husk necessitates no pretreatment; it is eco-friendly and low-cost, and that it has a satisfying biosorption capacity.

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Indirect Determination of Ascorbic Acid by Atomic Absorption Spectroscopy

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Abstract

A new and simple method followed by atomic absorption spectrometry has been developed for indirect determination of ascorbic acid (AA). The proposed method was based on the oxidation of AA to dehydroascorbic acid with Cu^{2+} cation (200mgL^{-1}) in an ammonium thiocyanate solution at pH 2.4. AA reduces Cu^{2+} to Cu^{+} followed by the precipitation of Cu^{+} with SCN^{-} . Then, the excess of Cu^{2+} in the solution was measured by the atomic absorption spectrometry. The results showed that AA can be sensitively measured in the linear range of 2.0 to 40.0mgL^{-1} with the detection limit of 1.5mgL^{-1} . The relative standard deviation (%RSD) was 0.319 in 7 determination of 2.0mgL^{-1} AA. Finally, the method was successfully used for the determination of AA in tablets containing various amounts of AA.

Keywords: Ascorbic acid, indirect determination, atomic absorption spectroscopy

1. Introduction

Ascorbic acid (AA) is one of the important vitamins which participates in a great variety of biological events concerning electron transport reaction, hydroxylation, and the oxidative catabolism of aromatic amino acids. Measuring the concentration of some chemical markers commonly assesses food determination and product quality: AA is one such indicator [1].

AA is considered to be essential for the development and regeneration of muscles, bones, teeth and skin. Also it has been

identified as a radical scavenger in vivo. AA or vitamin C is present naturally in a wide range of foods particularly fruits and vegetables. But AA has limited stability and may be lost from foods during storage, preparation and cooking. In some foods, it is purposely added to attract consumers and to act as an antioxidant [2] to prolong the shelf-life of the commercial products. Some pharmaceutical preparations add AA to their products as a supplementary source of vitamin C in human diets [3].

The therapeutic importance of AA has prompted many researchers to develop methods for its determination in such samples as well as in pharmaceuticals [4- 6][7]. So, it is very important to design a simple, selective

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and sensitive method for the determination of AA in routine analysis. Many analytical techniques are available for direct or indirect determination of AA in different matrices such as titrimetry [8], spectrophotometry [9- 11], HPLC [12,13], enzymatic methods [14], fluorimetry [15,16], various electroanalytical techniques [17,18], chemiluminescence [19,20], kinetic methods [21], capillary zone electrophoresis and isotachopheresis [22,23]. A large number of papers have been published and presented on AA quantification. This shows the importance of this compound. Some valuable articles have also been reviewed the determination of AA [24- 28].

However, indirect determination of AA has also been reported. Among various methods, the special interest is on flame atomic absorption spectrometry (FAAS) [29- 33]. The main reason is its improved detection limits, low relative standard deviation and selectivity as well as sensitivity.

The present work describes for first time the details of the development of an indirect method for the determination of ascorbic acid with atomic absorption spectroscopy based on the oxidation of ascorbic acid with Cu^{2+} and consequently, the precipitation reaction of resulted Cu^+ with thiocyanate. The unreacted copper is determined with FAAS without using any separation method.

2. Experimental

2.1. Apparatus

The cation absorbance was measured with a Perkin Elmer atomic absorption spectrometer model AA-800 with an air-acetylene flame and 10 cm burner. The wavelength was set to 324.0 nm for Cu^{2+} with a spectral slit-width of 0.7 nm and a lamp current of 15 mA.

2.2. Reagents and solutions

All chemicals were of analytical reagent grade. Solutions of ammonium thiocyanate

and disodium EDTA were made from purified samples in doubly distilled water. Ascorbic acid stock solution of 1000 mg L^{-1} was prepared by dissolving 0.100 g of ascorbic acid (Merck) in double distilled water in 100-mL flask and diluting to the mark. In order to analyze real AA samples twenty tablets of vitamin C (Kruger) were weighed and ground into a fine powder. An accurately weighed powder equivalent to 100 mg of the active component was transferred into a 100-mL flask and dissolved in doubly distilled water and the mixture was shaken thoroughly for 5 min. Then it was mixed well and diluted to the mark with distilled water. An aliquot of this solution was diluted appropriately to obtain the working concentrations and analyzed under proposed procedure.

2.3. Procedure

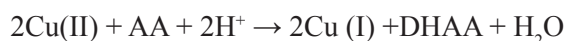
In this method, the 5.0 mL of copper sulfate solution (200 mg L^{-1}) was taken in the 100-mL beaker and 5.0 mL of ammonium thiocyanate solution (1% w/v) was added. Then the pH was adjusted to 2.4 with sodium hydroxide or hydrochloric acid, and then the exact known volume of ascorbic acid solution (50 mg L^{-1}) was added drop wise with constant stirring and heated on a heater stirrer for 15 min ($T = 70^\circ \text{C}$). The resulted precipitate was filtered through a sinter glass porosity crucible and washed three times with 0.1% ammonium thiocyanate solution and 20% (v/v) ethanol/water solution and diluted to 25 mL with distilled water. The amount of unreacted Cu^{2+} was determined by atomic absorption spectrophotometer at the wavelength of 324.0 nm. Hydrochloric acid was chosen for acidification of the solutions in the reaction vessel containing Cu^{2+} , SCN^- and AA. The various experimental parameters were optimized as well.

3. Results and discussion

Ascorbic acid (AA) is one of the natural

compounds having reducing characteristics. So, AA can be easily oxidized to dehydroascorbic acid (DHAA) by various agents. Cu (II) can oxidize AA during the following reaction:

(1)



The proposed method was based on the oxidation of AA with the excess amount of Cu (II) cation in hydrochloric acid medium, e.g. pH 2.4, and consequently, the precipitation reaction of resulted Cu^+ with thiocyanate⁴⁻ and then analysis of the unreacted copper by FAAS. It should be noted that the unreacted Cu(II) cannot precipitate with thiocyanate [34].

An increase in AA concentration causes more consumption of Cu^{2+} in the solution, so, the decrease in the measured absorbance of Cu^{2+} . The absorbance is found to be decreased linearly with increase in the concentration of AA.

3.1. Optimization of the experimental variables

A series of experiments were conducted to establish optimal analytical variables. All experimental parameters including pH, thiocyanate concentration, stirring time and temperature were optimized.

3.1.1. The influence of the amount of ammonium thiocyanate

Several aliquots of the standard solution $\text{Cu}^{2+} 200 \text{ mgL}^{-1}$ were transferred into a series of 25 mL standard flasks. Then, a volume of 5.0 mL of 50 mgL^{-1} AA solution was added to each flask followed by acidification by 2.0 mL of 0.1 molL^{-1} hydrochloric acid, and then different amounts of 1.0 % thiocyanate was added and the contents were diluted to the mark with distilled water and mixed well. When this solution was heated, precipitation of copper (I) thiocyanate began a few minutes and was complete in 15 min. The amount of unreacted

Cu^{2+} was determined by atomic absorption spectrophotometer at the wavelength of 324.0 nm. Blank was prepared similarly omitting the AA and its absorbance was measured against distilled water. The decrease in absorbance corresponding to consumed Cu^{2+} and in turn, to AA concentration, obtained by subtracting the absorbance of AA solution from the corresponding blank. The relationship between thiocyanate amount and the decrease in the measured absorbance of Cu (II) is shown in Fig. 1.

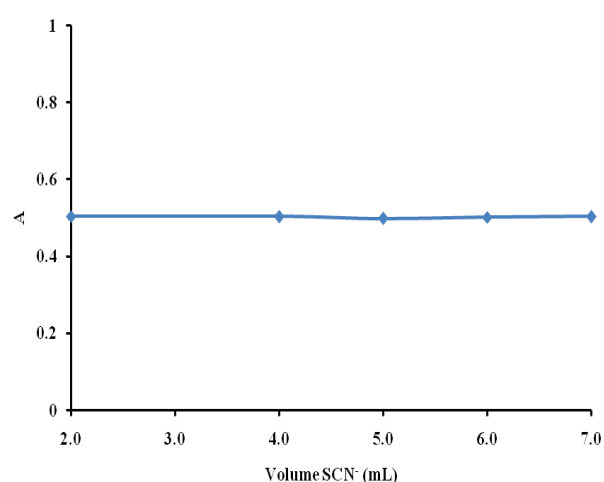


Fig. 1. Influence of the amount of ammonium thiocyanate (1.0%), $[\text{Cu (II)}] = 16 \text{ mgL}^{-1}$, Ascorbic Acid = 4.0 mgL^{-1} , Temp. = 70°C , Stirring time = 15.0 min, at $\lambda_{\text{max}} = 324.0 \text{ nm}$.

3.1.2 The effect of pH

As implies from equation (1), the reaction between Cu^{2+} and AA as well as the reduction potential of AA depends on the pH of the solution. At pH values higher than 5.0, the rate of copper reduction is much decreased and the precipitation is not completed even after a long time of the reaction [34].

Based on the above reaction an acidic environment is required, care should be taken that the concentration of the acid will give optimum performance. The response of oxidation was studied by using different HCl concentrations. The effect of pH value between 1.0 and 6.47 was evaluated (Fig. 2). The analytical signal decreases as the pH increases. There was increase in absorbance,

when pH value was decreased below 2.38 to 1.0, so the pH 2.38 was chosen as optimum.

Fig. 2 shows the influence of pH on the unreacted Cu^{2+} on condition that 5.0 mL of 50.0 mg/L ascorbic acid is added.

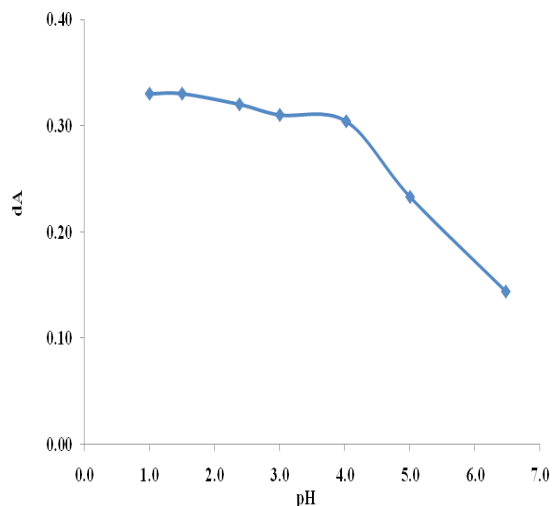


Fig. 2. Optimization of pH, at 5.0cc ammonium thiocyanate (1.0%), $[\text{Cu}(\text{II})] = 16 \text{ mg l}^{-1}$, Ascorbic Acid = 4.0 mg l^{-1} , Temp. = 70°C , Stirring time = 15.0 min, at $\lambda_{\text{max}} = 324.0 \text{ nm}$.

3.1.3. Stirring times

Effect of stirring time was also studied. It is from the data shown in Figure 3 that the reaction is completed in 10 min, so as to ensure completion of the reaction between AA and Cu^{2+} , time will choose 15 min. (Fig. 3).

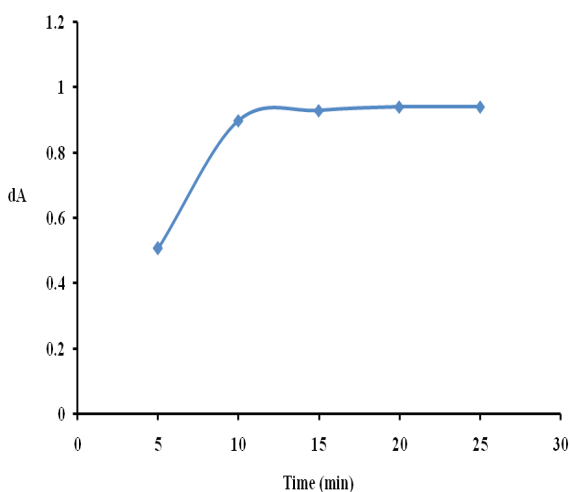


Fig. 3. Influence stirring time, at pH=2.38, 5.0cc ammonium thiocyanate (1.0%), $[\text{Cu}(\text{II})] = 16 \text{ mg l}^{-1}$, Ascorbic Acid = 4.0 mg l^{-1} , Temp. = 70°C , at $\lambda_{\text{max}} = 324.0 \text{ nm}$.

3.1.3. Effect of temperature

The effect of temperature on the consumption of Cu^{2+} is shown in Fig. 4.

The measured absorption of Cu^{2+} decreases with the increase in temperature. As expected, we found that at higher temperatures, the solubility of the precipitate increases, but due to the difficult work at higher temperatures of 70°C , this temperature to select the optimum temperature.

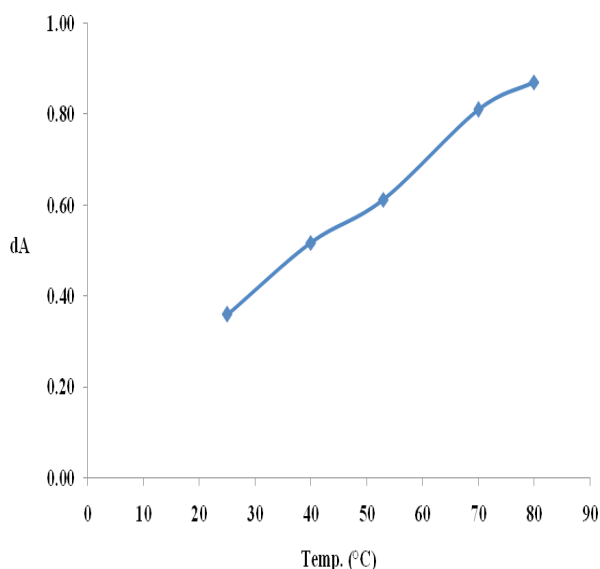


Fig. 4. The effect of temperature, at pH=2.38, 5.0cc ammonium thiocyanate (1.0%), $[\text{Cu}(\text{II})] = 16 \text{ mg l}^{-1}$, Ascorbic Acid = 4.0 mg l^{-1} , Stirring time = 15.0 min, at $\lambda_{\text{max}} = 324.0 \text{ nm}$.

3.1.4 Calibration Curve

A calibration curve is constructed by the recommended procedure in optimum condition (Fig. 6). A good linear relationship is observed between the unreacted of $\text{Cu}(\text{II})$ and the added of ascorbic acid to the solution. The linear equation for the calibration graph drawn at the wavelength of 324.0 nm as described in the section 2.2 was

$$\Delta A = 0.014C + 0.125$$

Where C is the part per million concentration of AA, with correlation coefficient $R^2 = 0.998$.

The calibration curve for the

determination of ascorbic acid was prepared according to the general procedure under the optimum conditions developed above (Fig. 5). The linearity was obtained in the range of 2.0-40.0 mg L⁻¹ of ascorbic acid with a correlation coefficient of 0.998. The detection limit of the proposed method (calculated as 3σ) was obtained to be 1.5 mgL⁻¹. The relative standard deviation of AA determination (4.0mgL⁻¹) was found to be 0.32% (n=8) (Fig. 5).

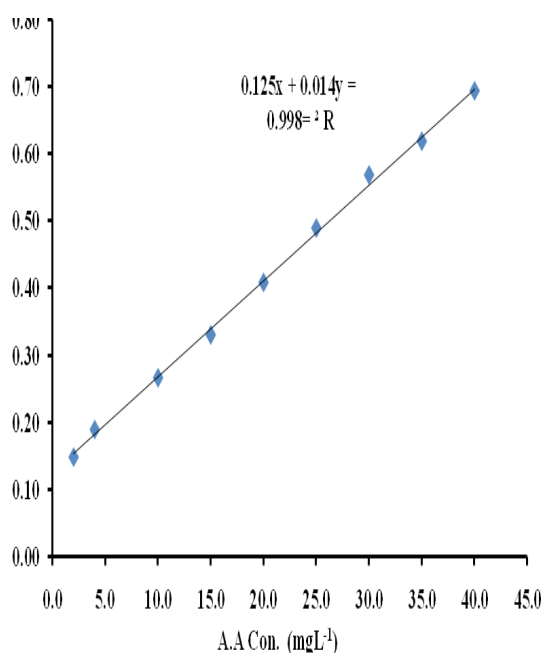


Fig. 5. Calibration curve for AA determination

3.1.5. Sample analysis

Treatments of samples Vitamin C tablets several tablets of vitamin C drug are accurately weighed ground and powdered. A given amount of this powder is transferred into a volumetric flask and diluted to the mark. The content of the flask is shaken for about 10 min. Then it is filtered and the first portion of the filtrate is rejected. This solution is further diluted to adjust the concentration to meet the requirement of the experimental conditions adopted.

4. Conclusions

Ascorbic acid can be analyzed at the DL 1.5μg ml⁻¹ level when reacting with Cu (II)

with the formation of the Cu (I) –thiocyanate precipitate, and concentration and indirect measurement AA. This is a very sensitive, simple and selective one-step method, suitable for laboratory routine control and can be carried out directly without any pre-treatment of the samples.

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Prediction of PVT Properties of Pure Refrigerants Using ISM Equation of State

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Abstract

A three-parameter cubic equation of state has been proposed for predicting PVT of pure refrigerants such as R236ea, R236fa, R245fa, R245ca, R218, R227ea, and R717, from freezing point up to critical point temperature and pressures up to 650 atm. We explore the theory of the equation of state from the view point of Ihm–Song–Mason (ISM) equation of state, which has been derived on the basis of statistical mechanical perturbation theory, and is characterized by three temperature dependent parameters, a , b , B_2 , and a free parameter λ . The second virial coefficients are calculated from a correlation based on the heat of vaporization, ΔH_{vap} , and the liquid density at the normal boiling point, ρ_{nb} . $\alpha(T)$ and $b(T)$ can also be calculated from second virial coefficients by a scaling rule. The theory has considerable predictive power, since it permits the construction of the PVT surface from the heat of vaporization and the liquid density at the normal boiling point. The results indicate that the liquid densities can be predicted with very good agreement over a wide range of temperatures, 100–400 K.

Keywords: Equation of State, Correlation, Heat of Vaporization, Saturation Liquid Density of Refrigerants

1. Introduction

Accurate knowledge and prediction of the thermophysical properties of refrigerants, is of great importance to evaluate the performance of refrigeration cycles and to determine the optimum composition of new working fluids in pure and mixture states. The development of models for representation and prediction of physical properties and phase equilibria as well as the improvement of current equations of state (EOS) is of particular interest for

the refrigeration industry. Thermodynamic properties of the long-known refrigerants and the new refrigerants are the key data needed for the calculation of refrigeration cycles and for designing refrigeration and air-conditioning equipment.

In 1992, Ihm, Song and Mason [1] presented an EOS based on statistical-mechanical perturbation theory for mixtures of fluids. The second virial coefficient, which characterizes binary interactions between atoms and molecules, plays an important role in the EOS, as a source of a scaling factor for calculating the other two temperature-

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dependant parameters, $\alpha(T)$ and $b(T)$. It will be shown that by knowing the second virial coefficient, the prediction of the entire pressure-volume-temperature (PVT) surface of fluids can be achieved at least for state points less than the critical temperature. Knowledge of the binary intermolecular potential energy between atomic and molecular constituents of the systems [1, 2] makes it possible to calculate second virial coefficients. Unfortunately, there are no exact intermolecular potential energies (except for some simple gases) for real fluids.

Therefore it seems reasonable to find other methods to evaluate the second virial coefficient. Of course, the experimental second virial coefficient is another good source for using the EOS. But experimental second virial coefficients have not been derived for all systems over a wide range of temperatures. The most generally useful method for prediction of the volumetric properties of fluids, such as the second virial coefficient, is the use of the hypothesis of corresponding states, which came originally from van der Waals in his well-known EOS.

Many investigations have attempted to extend the applicability of equations of state for pure and liquid mixtures [2-12] with even more readily available parameters to cover a wide range of substances, even for those which experimental data such as the second virial coefficient or the intermolecular potential energy are not yet available. In the absence of the accurate values of the second virial coefficients, there are several correlation methods, usually based on a principle of corresponding states, by which $B_2(T)$ can be estimated with reasonable accuracy.

2. Theory

Starting from the pressure equation [13] and applying the Weeks–Chandler–Andersen [14] decomposition of the potential energy function, Song and Mason [15, 16] obtained

an analytical equation of state of the form

$$\frac{P}{\rho kT} = 1 + \frac{(B_2 - \alpha)\rho}{1 + 0.22\lambda b\rho} + \frac{\alpha\rho}{1 - \lambda b\rho} \quad (1)$$

for nonpolar and slightly polar fluids. Here P is the pressure, ρ is the molar (number) density, B_2 is the second virial coefficient, α is the contribution of the repulsive forces to the second virial coefficient, b is a temperature dependent parameter analogous to the van der Waals covolume, kT is the thermal energy of one molecule, and λ is an adjustable parameter. The parameters B_2 , α , and b are all temperature dependent and can be evaluated by knowing the intermolecular forces. However, such forces are almost never known with sufficient accuracy, except for noble gases [17]. If the values of the three parameters are known, the free parameter λ can be determined experimentally from high-density PVT data such as a saturated liquid density. Also the major problem now is to find the three dependent parameters B_2 , α and b . In the following, we describe a procedure for the determination of these temperature-dependent parameters using a macroscopic corresponding-states-correlation.

3. Correlation procedure

The second virial coefficient $B_2(T)$ plays a central role in the application of Eq. (1). It is used both directly and as the source of scaling constants for the calculation of $\alpha(T)$ and $b(T)$. The minimum input information needed to use Eq. (1) consists of the value of $B_2(T)$ plus some high-density data to fix the value of an adjustable shape constant in $G(b\rho)$. For many fluids, neither accurate potential functions nor experimental values of $B_2(T)$ over the whole range of temperature are available. In the absence of accurate values of $B_2(T)$, there are several correlation schemes, usually based on the principle of corresponding states, by which $B_2(T)$ can be estimated with reasonable

accuracy. To determine the parameter $B_2(T)$, we have used the following correlation [11]:

$$B\rho_{nb} = 0.403891 - 0.076484(\Delta H_{vap}/RT)^2 - 0.0002504(\Delta H_{vap}/RT)^4 \quad (2)$$

Once the $B_2(T)$ values are known, the parameters $\alpha(T)$ and $b(T)$ of the equation of state are derived from the second virial coefficient [11]:

$$\alpha\rho_{nb} = a_1 \exp[-c_1(RT/\Delta H_{vap})] + a_2 \left\{ 1 - \exp[-c_2(\Delta H_{vap}/RT)^{1/4}] \right\} \quad (3)$$

$$b\rho_{nb} = a_1 [1 - c_1(RT/\Delta H_{vap})] \exp[-c_1(RT/\Delta H_{vap})] + a_2 \left\{ 1 - [1 + 0.25c_2(\Delta H_{vap}/RT)^{1/4}] \exp[-c_2(\Delta H_{vap}/RT)^{1/4}] \right\} \quad (4)$$

$$a_1 = -0.1053$$

$$c_1 = 5.7862$$

$$a_2 = 2.9359$$

$$c_2 = 0.7966$$

where ρ_{nb} and ΔH_{vap} are the liquid density and heat of vaporization at the normal boiling point respectively. The correlations cover a wide range of temperatures.

4. Results and Discussion

In this work Ihm-Song-Mason equation of state (ISM EOS) for pure refrigerants [18] is applied to calculate saturated liquid densities. Actually the purpose of this work is to show how the ISM equation of state can be used with even less input information for

refrigerants. Two constants are needed for each pure component, ΔH_{vap} and ρ_{nb} , which are readily available, and there is seldom any difficulty in determining them; only simple measurements are needed if values cannot be found in the literature.

Three temperature-dependent parameters of the ISM EOS are calculated with Eqs. (2)-(4). The free parameter λ of Eq. (1) for each pure refrigerant is calculated by using boiling-point data. This method for determining λ makes the whole procedure self-correcting, because if the input values ΔH_{vap} and ρ_{nb} at the normal boiling point are not accurate, the effects will be largely compensated by this adjustable parameter. Once the value of the constant λ is determined, the entire volumetric behavior of the given fluids is established. Values obtained for λ as well as the heat of vaporizations and liquid densities at the normal boiling point for refrigerants are given in Table 1.

We considered the refrigerants that widely used currently and also substitutions of harmful refrigerant such as R12, R114, R22 and R502.

In the search fluids for potential applications as refrigerants in high-temperature heat pumps, centrifugal chillers, and chemical blowing agents, two new refrigerants, namely, 1,1,1,2,3,3-hexafluoropropane (R236ea), and 1,1,1,3,3,3-hexafluoropropane (R236fa), are among the most promising. The refrigerants have virtually zero potential to deplete the stratospheric ozone, low global warming

Table 1. Parameters used for pure refrigerants.

Refrigerant	Formula	T_{nb} (K)	ρ_{nb} (kg.m ⁻³)	$\Delta H_{vap}/R$ (K)	λ
R236ea ^a	CF ₃ CHFCHF ₂	279.3	1482.6	3020.5	0.408
R236fa ^a	CF ₃ CH ₂ CF ₃	271.7	1444.7	2931.8	0.408
R245fa ^a	CF ₃ CH ₂ CHF ₂	288.1	1365.7	3171.3	0.411
R245ca ^a	CHF ₂ CF ₂ CH ₂ F	298.3	1386.0	3240.2	0.409
R218 ^b	C ₃ F ₈	236.4	1603.0	2351.9	0.392
R227ea ^b	CF ₃ CHFCF ₃	256.7	1535.0	2695.4	0.403
R717 ^b	NH ₃	239.9	682.0	2804.2	0.421

^a from Ref. [19].

^b from Ref. [20].

potential, and are completely nonflammable over a wide range of concentrations in air at temperatures up to 323 K, and no unusual toxicity has been indicated in limited toxicity testing. Through thermodynamic evaluation and experimental tests, R236ea has been demonstrated to have high potential as an alternative for R-114 [21]. Calculated of saturated liquid densities for R236ea and R236fa is shown in Figures 1 and 2.

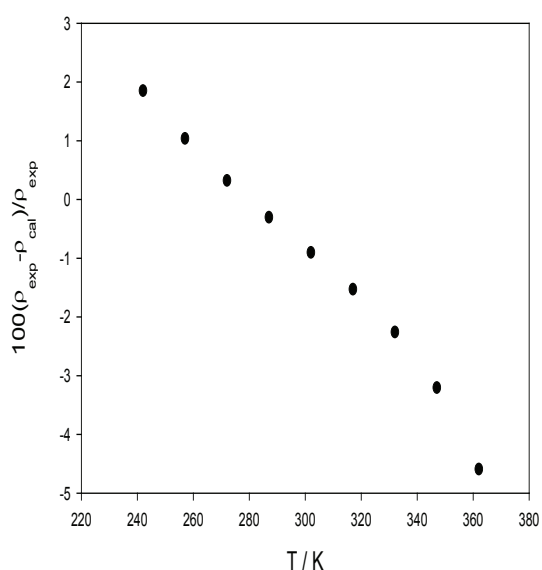


Fig. 1. Deviation plot for calculated saturated liquid densities by ISM EOS as a function of temperature, for R236ea and compared with Ref. [19].

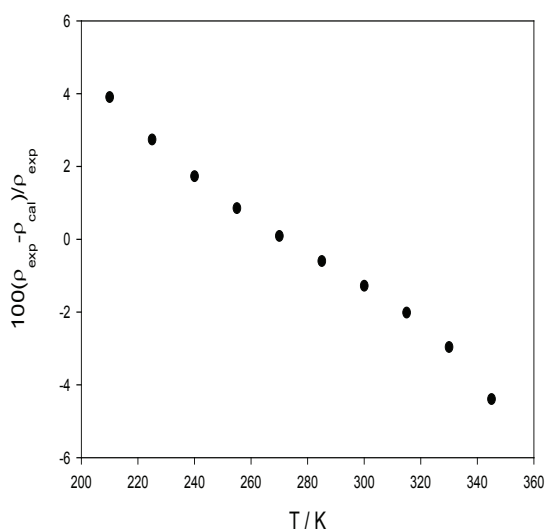


Fig. 2. The same as fig.1. for R236fa.

1,1,2,2,3-pentafluoropropane (R245ca) is currently considered as a potential replacement for chlorine-containing compounds used in chillers, such as R-11 [22].

1,1,1,3,3-pentafluoropropane (R245fa), a non-flammable, low-pressure (relative to R-134a) HFC refrigerant has been introduced for the foam blowing industry [23, 24]. The relatively high critical temperature of this fluid means that it would be an efficient working fluid for air-conditioning equipments [25]. The results for R245ca and R245fa are shown in Figures 3 and 4.

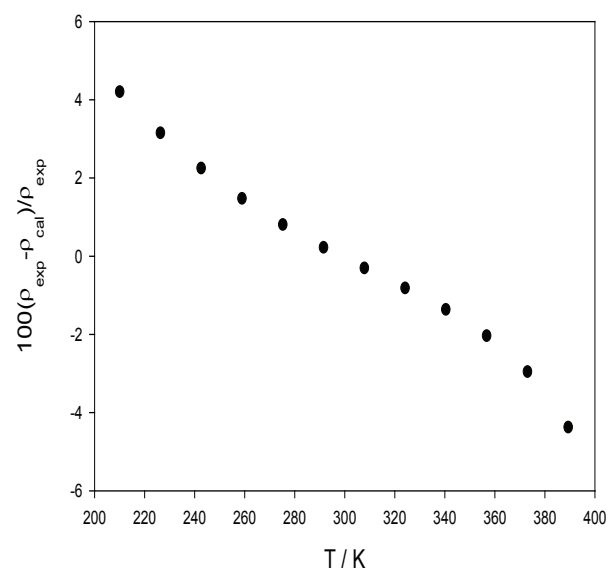


Fig. 3. The same as figure 1. for R245ca.

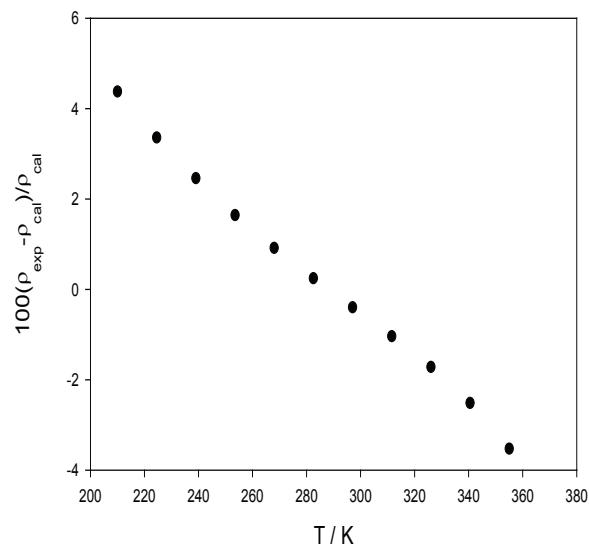


Fig. 4. The same as figure 1. for R245fa.

1,1,1,2,3,3,3-heptafluoropropane (R227ea), which is chlorine-free, can be considered as a possible alternative refrigerant. It is intended as a potential alternative for R12 and R114 for units with high condensing temperatures, and also blends containing R227ea are potential alternatives to R22 and R502. It can be used in fire suppression, sterilization, and propellant applications [26].

Octafluoropropane (R218) is used in mixture with oxygen in semiconductor applications as an etching material for SiO₂ layers, and also is a component in refrigeration mixtures.

Ammonia (R717) is perhaps most well recognized as a household cleaner, and makes another important contribution to daily life as an industrial refrigerant. More recently, ammonia refrigeration systems have been used for air conditioning in publicly accessed buildings and increasing output efficiencies for power generation facilities.

Figures.5-7 are deviation plots for R227ea, R218, and R717.

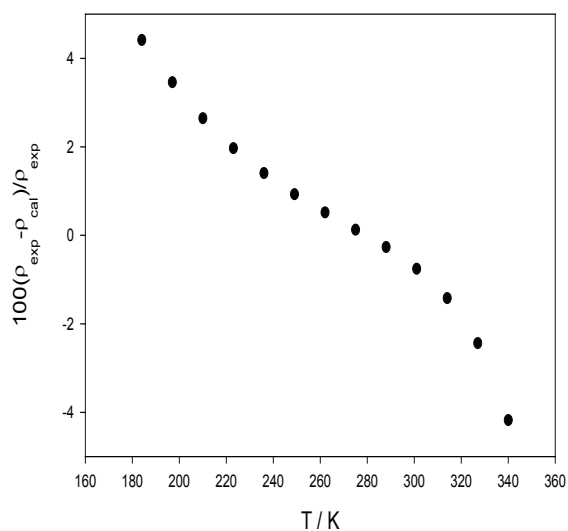


Fig. 5. The same as fig. 1. R227ea.

As shown in Figures 1-7, the trend of percent deviation, from positive to about zero then becoming negative is due to the particular choice of λ . All of measurements are from freezing point up to critical temperature

and at the boiling temperature at which λ is determined the deviation is around zero.

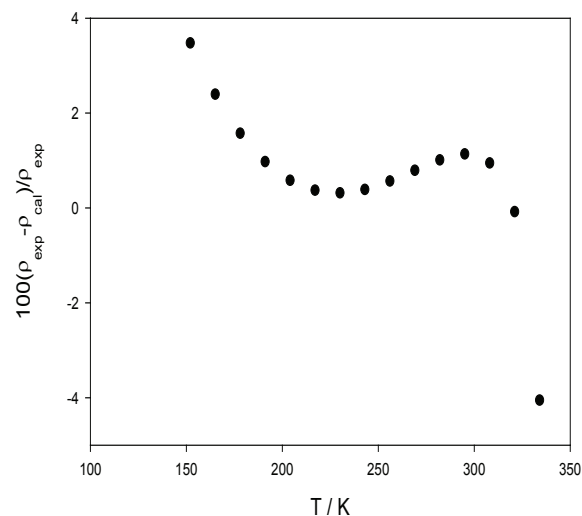


Fig. 6. The same as fig. 1. for R218.

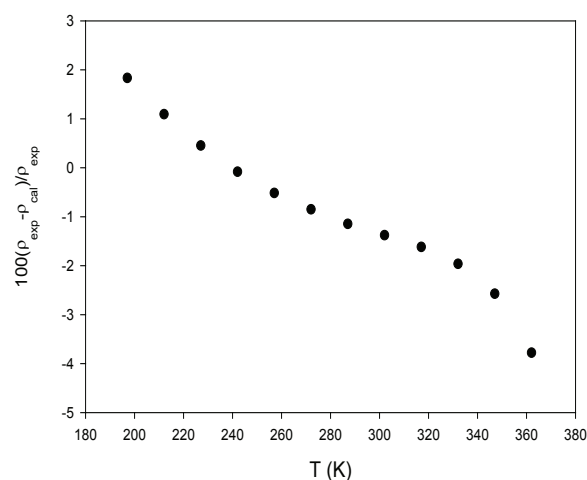


Fig. 7. The same as fig. 1. for R717.

As the figures show there is very good agreement between the calculated values by ISM equation of state and experimental results [19] for pure refrigerants over a wide range of temperatures and pressures.

5. Conclusions

A cubic-perturbed equation of state has been proposed that can predict PVT properties for pure refrigerants over a wide range of

temperatures and pressures. An important problem in the thermodynamics of fluids is to derive analytical EoS for real substances, i.e., to obtain explicit relations for the thermodynamic variables in terms of relevant molecular features. Such relations allow us to understand the specific behavior of a real substance in terms of its molecular features and, on practical terms, to use efficiently the usually limited knowledge of the properties of a substance to predict their values in other states. So far, this goal has been partially attained by the ISM EoS. Hence, a conclusion central to our study is that it seems to describe an interesting example of the application of ISM EoS to calculate the molar volume pure refrigerants. The second virial coefficients are calculated from a correlation based on the heat of vaporization, ΔH_{vap} , and the liquid density at the normal boiling point, ρ_{nb} . $\alpha(T)$ and $b(T)$ can also be calculated from second virial coefficients by a scaling rule.

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The DFT Study of Oxygen Adsorption on Pristine and As-Doped of the (4, 4) Armchair Models BNNTs

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Abstract

In this work, the effects of As-doped on the adsorption of oxygen gas on the outer and inner surface of boron nitride nanotube (BNNTs) is investigated. The structural parameters, quantum properties involving: bond length, bond angle, HOMO-LUMO orbital, gap energy, electron affinity, electronegativity, chemical potential, global hardness, global softness and NMR parameters of BNNTs are calculated at different configurations of O₂ adsorption on the outer and inner surface of BNNTs by performing density functional theory (DFT) using Gaussian 03 package of program. Our results reveal that the adsorption energy of all models is exothermic and the E_{ads} value in (A and B) undoped models of BNNTs is larger than those of the other models. The results show that As-doped impurities and O₂ adsorption decrease the adsorption energy of O₂ gas on the surface of BNNTs and the gap energy between HOMO-LUMO orbital and increase the conductivity of nanotube.

Keywords: BNNTs, Adsorption O₂, As-doped, DFT, NMR

1. Introduction

Soon after the theoretical and experimental approach on BNNTs [1, 2], Considerable theoretical and experimental efforts have been devoted to investigate the electrical and structural properties and applications of (BNNTs) [3–8]. The structural properties of BNNTs are similar CNTs, while their electronic properties are quite different from CNTs,

however they exhibit only semiconducting properties independent of their chirality and diameter with wide band gaps ranging from 4 to 5.5 eV. Like diamond, boron nitride acts as an electrical insulator, but it is an excellent conductor of heat [9-15]. Recent experimental and theoretical studies have a strong interest on the phenomenology of gas molecules such as O₂, NO₂, NH₃, and many other gases, at ambient temperature on nanotube [15-20]. In the last years, several theoretical studies have been performed to study the adsorption of O₂ on single-walled carbon nanotubes (SWNT)

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using density functional theory (DFT) [21-26]. Recent researches show that interaction of oxygen with nanotubes have always been an interesting and fascinating, subject for the scientific community for both fundamental and practical reasons, as well as for the possible applications and chemical manufacturing processes in nano device technologies and in chemical sensors [27-34]. Following our previous research on the electrical structural and NMR parameters SiC-doped AIPNTs, Ga, Al, N, Ge, As doped BPNTs [35-38], in the present work, we investigate the sensitivity of BNNTs toward O₂ molecules at different positions of outside and inside of BNNTs and the effect of As doped on the adsorption. The chemical shielding (CS) tensors originating at the sites of half-spin nuclei, structural properties and quantum parameters involving: HOMO-LUMO orbital, gap energy, other quantum molecular descriptors at different situation of O₂ adsorption inside and outside of BNNTs are investigated by performing density functional theory (DFT) using Gaussian 03 package of program.

2. Computational methods

The structural and electrical properties of (4, 4) armchair models of undoped and As-doped of BNNTs (see Figs. 1-2) with adsorption of O₂ on the surface of nanotubes are investigated by density function theory at B3LYP level of theory using the Gaussian 03 set of programs [39-40]. After optimizing all consider structures of nanotubes, the chemical shielding (CS) tensors at the sites of ¹¹B, ¹⁴N nuclei based on the gauge included atomic orbital (GIAO) approach and same level of theory [41]. The calculated CS tensors in principal axes system (PAS) ($\sigma_3 > \sigma_2 > \sigma_1$) are converted to measurable NMR parameters,

chemical shielding isotropic (CSI) and chemical shielding anisotropic (CSA) by using equations (1) and (2), respectively [35-38].

$$CSI(ppm) = \frac{1}{3}(\sigma_1 + \sigma_2 + \sigma_3) \quad (1)$$

$$CSA(ppm) = \sigma_3 - (\sigma_1 + \sigma_2)/2 \quad (2)$$

Adsorption energy (E_{ads}) of oxygen gas on the surface of pristine and As-doped BNNTs was calculated as follow:

$$E_{ads} = E_{BNNTs-O_2} - (E_{BNNTs} + E_{O_2}) + BSSE \quad (3)$$

Where $E_{BNNTs-O_2}$ was obtained from the scan of the potential energy of the BNNTs-O₂, E_{BNNTs} is the energy of the optimized BNNTs structure, and E_{O_2} is the energy of an optimized O₂ and BSSE is base set superposition errors. The quantum molecular descriptors: electronic chemical potential (μ), global hardness (η), electrophilicity index (ω), energy gap, global softness (S), electronegativity (χ) and maximum amount of electronic charge, ΔN , of the nanotubes [42-45] were calculated as the following equations indicate:

$$\mu = -(I + A)/2 \quad (4)$$

$$\mu = -\chi \quad (5)$$

$$\omega = \mu^2 / 2\eta \quad (6)$$

$$\eta = (I - A)/2 \quad (7)$$

$$S = 1/2\eta \quad (8)$$

$$E_{gap} = E_{LUMO} - E_{HOMO} \quad (9)$$

$$\Delta N = \frac{-\mu}{\eta} \quad (10)$$

Where $I(-E_{HOMO})$ is the ionization potential and $A(-E_{LUMO})$ the electron affinity of the molecule. The electrophilicity index is a measure of the

electrophilic power of a molecule.

3. Results and discussion

3.1 Structural Properties

In this work, we begin our study with oxygen gas adsorption on the outer and inner surface of pristine and As-doped (4, 4)

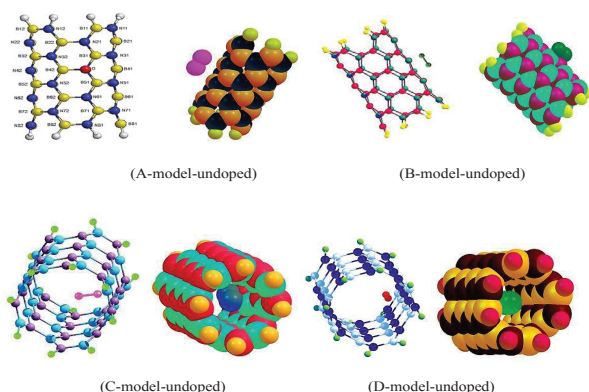


Fig. 1 2D views of O₂ adsorption on the undoped of (4, 4) armchair model of BNNTs;

Model A shows the vertical adsorption of O₂ gas on the outer surface of nanotube.

Model B shows the vertical adsorption of O₂ gas on the inner surface of nanotube.

Model C shows the parallel adsorption of O₂ gas on the outer surface of nanotube.

Model D shows the parallel adsorption of O₂ gas on the inner surface of nanotube

armchair BNNTs with the diameters 5.4 Å. For this aim, we consider four models (A-D) for adsorption of O₂ gas on the surface of nanotube. Model A shows the vertical adsorption of O₂ gas on the outer surface of nanotube, Model B indicates the vertical adsorption of O₂ gas on the inner surface of nanotube, Model C shows the parallel adsorption of O₂ gas on the outer surface of nanotube, and Model D demonstrates the parallel adsorption of O₂ gas on the inner surface of nanotube (See Figures 1-2). The structural properties such as bond length and

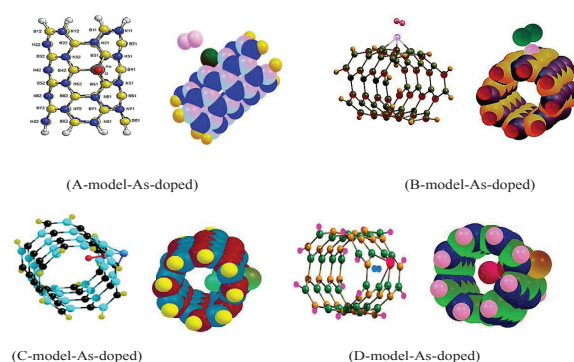


Fig. 2. 2D views of O₂ adsorption on the As-doped of (4, 4) armchair model of BNNTs; For (A-D) models (see Fig. 1).

Table 1. Structures parameters of O₂ adsorption on undoped and As-doped of (4, 4) armchair models of BNNTs, first value for undoped and second value for As-doped of (A-D) models of adsorption. see Fig. 1,2)

Bondlength (Å)	Unadsobed	Model (A)	Model (B)	Model (C)	Model (D)
B ₄₂ -N ₄₁ /As	1.46 [2.01]	1.45[2.01]	1.53 [2.01]	1.46[2.17]	1.52[2.15]
B ₃₁ -N ₄₁ /As	1.46[1.98]	1.46[1.98]	1.52[2.02]	1.46[2.14]	1.52[1.98]
B ₅₁ -N ₄₁ /As	1.46[1.97]	1.45[1.97]	1.64[1.99]	1.45[3.13]	1.60[2.05]
B ₄₂ -N ₃₂	1.46 [1.45]	1.45[1.44]	1.43 [1.44]	1.45 [1.45]	1.43 [1.47]
B ₃₁ -N ₂₁	1.46 [1.46]	1.46[1.46]	1.45 [1.46]	1.46 [1.54]	1.44 [1.47]
B ₄₂ -N ₅₂	1.46 [1.45]	1.45[1.44]	1.42 [1.44]	1.45 [1.45]	1.42 [1.45]
B ₅₁ -N ₆₁	1.46 [1.45]	1.45[1.45]	1.51 [1.44]	1.45 [1.42]	1.47 [1.49]
B ₃₁ -N ₃₁	1.46 [1.44]	1.45[1.44]	1.41 [1.44]	1.45 [1.46]	1.42 [1.43]
B ₅₁ -N ₅₁	1.46 [1.44]	1.45[1.44]	1.50 [1.44]	1.45 [1.41]	1.48 [1.49]
Bond angle(°)					
<B ₃₁ -N ₄₁ /As-B ₄₂	115[88]	115[88]	110[90]	116[78]	123[96]
<N ₄₁ /As-B ₄₂ -N ₃₂	118[118]	119[118]	116[117]	119[107]	113[112]
<N ₂₁ -B ₃₁ -N ₄₁ /As	120[114]	120[114]	117[114]	120[68]	116[110]
<N ₄₁ /As-B ₄₂ -N ₅₂	119[119]	120[119]	119[117]	120[133]	117[109]
<N ₆₁ -B ₅₁ -N ₄₁ /As	120[114]	119[114]	111[113]	118[96]	115[106]
<B ₅₁ -N ₄₁ /As-B ₄₂	116[87]	119[88]	119[91]	117[63]	115[89]
<B ₅₁ -N ₄₁ /As-B ₃₁	120[95]	119[95]	115[98]	119[49]	122[98]
<N ₄₁ /As-B ₃₁ -N ₃₁	118[124]	116[124]	119[122]	119[147]	114[118]
<N ₅₁ -B ₅₁ -N ₄₁ /As	119[125]	115[125]	130[124]	120[120]	113[116]

bond angle of pristine and four adsorption models are given in Table 1. Comparing results reveal that the bond length of $B_{42}-N_{41}, B_{31}-N_{41}, B_{51}-N_{41}$ of (B, D) undoped models increase from 1.46 to 1.52, 1.52, and 1.60 Å respectively. On the other hand, the adsorption of O_2 on the B model caused that the bond length of $B_{51}-N_{61}, B_{51}-N_{51}$ increase from 1.46 to 1.51 and 1.50 Å respectively, due to interaction π electron of O_2 gas with nanotube. And also the s-character of the hybridized orbitals decrease which leads to an increase in the interaction of nanotube orbitals with the O_2 orbitals. With doping As in the B41 nuclei of nanotube, the $B_{42}-N_{41}, B_{31}-N_{41}, B_{51}-N_{41}$ bond length increase from 1.46 to 2.01, 1.98 and 1.97 Å respectively, because the radius of As is more than B atoms. The adsorption of O_2 gas increases significantly the bond length of neighbourhood As-doped. The increase of bond length on the C model is larger than other models. The bond angles of neighbourhood As-doped of BNNTs in all models decrease from pristine models due to more radius of As respect B atoms. The bond angle of $\langle B_{31}-N_{41}/$

$As-B_{42}$ of B model of undoped nanotube decrease from 115 to 110° and at D model of undoped this bond angle increase to 123°. The bond angles $\langle B_{31}-N_{41}/As-B_{42}, \langle N_{21}-B_{31}-N_{41}/As, \langle B_{51}-N_{41}/As-B_{42}$ and $\langle B_{51}-N_{41}/As-B_{31}$ of C model decrease from original values in As-doped of nanotube and $\langle N_{41}/As-B_{31}-N_{31}$ of this model increase significantly to 147° in As doped.

The results of adsorption energies between nanotube and O_2 gas calculated on Eqs. 3 are given in Table 2. The results show that the adsorption energy of all models is exothermic and at the (A and B) models the adsorption energy values are more than other models. On the other hand with doping As, the adsorption energy decreases largely from undoped model, this result demonstrates that As-doped is not favorable for O_2 adsorption in all models. Base set superposition error for all models is 0.01 eV.

3.2 Electronic and quantum properties

Table 2 presents the results for the HOMO, LUMO, gap energies, and quantum

Table 2. Quantum parameters of O_2 adsorption on pristine and As-doped of (4, 4) armchair models of BNNTs.

	BNNT(4,4)										
	O_2	pristine	As-doped	Model (A)		Model (B)		Model (C)		Model (D)	
				Un doped	As Doped	Un doped	As Doped	Un doped	As Doped	Un doped	As Doped
E(ads)/kcal/mol	-	-	-	-19.45	-0.27	-19.37	-0.13	-18.87	-0.12	-17.41	-1.36
E(Bsse)/ev	-	-	-	0.01	0.012	0.01	0.03	0.01	0.02	0.01	0.02
E(HOMO)/ev	-6.81	-6.32	-6.38	-6.23	-5.04	-6.29	-5.29	-6.47	-6.06	-6.32	-6.16
E(LUMO)/ev	-4.77	-0.11	-0.75	-4.18	-3.05	-1.68	-1.96	-4.79	-2.01	-1.95	-3.87
E(gap)/ev	2.04	6.21	5.63	2.05	1.99	4.61	3.33	1.68	4.05	4.37	2.29
η/ev	1.02	3.11	2.82	1.03	0.99	2.31	1.67	0.84	2.02	2.19	1.14
S/(ev)⁻¹	0.49	0.16	0.18	0.48	0.51	0.22	0.30	0.59	0.25	0.23	0.44
μ/ev	-5.79	-3.22	-3.57	-5.21	-4.05	-3.99	-3.63	-5.63	-4.03	-4.14	-5.01
χ/ev	5.79	3.22	3.57	5.21	4.05	3.99	3.63	5.63	4.03	4.14	5.01
ω/ev	16.43	1.67	2.26	13.18	8.28	3.45	3.94	18.87	4.02	3.91	11.01
ΔN	5.68	1.03	1.27	5.06	4.09	1.73	2.17	6.70	1.99	1.89	4.39

parameters obtained by the DFT calculations and Eqs. (4-9). Calculated gap energies for the isolated nanotubes are 6.21 eV in pristine and 5.43 eV in As-doped models. With adsorbing O₂ gas on the outer surface of the nanotube, the gap energy between HOMO-LUMO orbital decrease from original values due to donor electron effects of O₂ gas. This lowering of gap energy with O₂ adsorption may be able to increase the reactivity of the O₂/BNNTs complex, and shows charge transfer to take place between the π electron of O₂ and BNNTs sidewall.

The electronic chemical potential (μ), global hardness (η) of O₂ adsorption on surface of BNNTs is presented in Table 2. The results show that, the chemical potential and global hardness decrease with decrease in gap energy. The results also show that the chemical potential and global hardness in C undoped model of nanotube is lower than other models. Therefore, we can predict that adsorbing O₂ decreases the stabilities of pristine nanotube. The comparison of electronegativity (χ) of the nanotubes reveals that with adsorbing O₂ the electronegativity increases from pristine models. The electronegativity of undoped C model is larger than other models and the electronegativity of As-doped B model is lower than other models. By bringing the O₂ gas and nanotubes together, electrons will flow from that of lower electronegativity atoms to that of higher electronegative atom. Therefore, the difference in electronegativity drives the electron transfer. As a result, electrons will flow from a definite occupied orbital in a nanotube and will go into a definite empty orbital in an O₂ molecule. The overlap between the exchanging orbitals will be critical in determining the energy changes. In addition, the values for gap energy and hardness for O₂ molecule is smaller than the nanotube; these

results lead that O₂ molecule having higher polarizability than the nanotubes. The amount of charge transfer (ΔN) between the O₂ molecule and (A-D) models of adsorption, as calculated using the Eq. (10) and given in Table 2. In all models, ΔN values are positive and indicate that O₂ molecule act as an electron acceptor. The ΔN values of undoped C model are significantly larger than other models and therefore in this model, the charge transfer from nanotube to O₂ gas is larger than other model.

3.3 NMR parameters

The NMR (CSI and CSA) parameters of ¹¹B and ¹⁴N nuclei for the pristine, As-doped of (4, 4) armchair BNNTs in presence of O₂-adsorption ((A-D) models Fig. 1, 2) are calculated by Eqs (1, 2) and given in Tables (3-6). A look at results of A model (Table 3) show that with doping As atom the CSI values of ¹¹B nuclei at the sites B31, B42, B51 decrease significantly from 82, 80 and 81 ppm to 61, 71, and 63 respectively. On the other hand, the CSA values of ¹¹B nuclei at the layers 1, 3, 5, 7 increase from undoped model and on the other layers increase. The direction of changes for isotropic and anisotropic chemical shielding because of difference in physical concept of these parameters is different. The CSI values of ¹⁴N nuclei at the N21, N32, and N61 with doping As decrease significantly from undoped model, due to donor electron effect of As-doped. The CSA values of ¹⁴N nuclei at the layers 1, 3, 5, 7 decrease from undoped model and the other layers increase.

In the B model, the CSI values at B31, B42, B51, B52 sites decrease largely from original values. The CSA values of ¹¹B nuclei at the layers 1, 3, 5, 7 are decreased from undoped model and the other layers increase, the similar results are shown for A model. The CSI values

Table 3. NMR parametres of O₂ adsorption on undoped and As-doped of (4, 4) armchair BNNTs, (A) model of Fig.1.

B-11 nuclei	CSI (ppm)		CSA (ppm)		N-14 nuclei	CSI (ppm)		CSA (ppm)	
	Undoped	Doped	Undoped	Doped		Undoped	Doped	Undoped	Doped
B ₁₁	80	84	18	37	N ₁₁	146	147	80	65
B ₁₂	80	80	19	34	N ₁₂	146	143	75	68
B ₁₃	80	80	20	31	N ₁₃	146	146	80	69
B ₁₄	80	80	19	32	N ₁₄	146	146	82	69
B ₂₁	84	86	34	28	N ₂₁	137	113	132	157
B ₂₂	84	82	33	27	N ₂₂	136	136	135	167
B ₂₃	84	84	34	30	N ₂₃	136	135	135	162
B ₂₄	84	84	34	30	N ₂₄	136	139	135	169
B ₃₁	82	61	15	29	N ₃₁	134	120	139	106
B ₃₂	82	83	15	25	N ₃₂	134	120	135	68
B ₃₃	82	81	15	24	N ₃₃	134	134	136	103
B ₃₄	82	83	15	26	N ₃₄	134	135	135	86
B ₄₁	82	83	35	26	N ₄₁ /As	124	-	164	-
B ₄₂	80	71	36	24	N ₄₂	140	138	138	167
B ₄₃	82	81	34	31	N ₄₃	140	140	137	162
B ₄₄	82	82	34	29	N ₄₄	140	142	138	163
B ₅₁	81	63	19	26	N ₅₁	141	126	141	113
B ₅₂	81	83	16	25	N ₅₂	139	125	138	67
B ₅₃	82	81	15	23	N ₅₃	140	139	137	105
B ₅₄	82	83	15	26	N ₅₄	140	141	136	88
B ₆₁	82	83	35	31	N ₆₁	117	112	165	152
B ₆₂	81	80	38	26	N ₆₂	134	135	137	164
B ₆₃	82	82	35	32	N ₆₃	134	134	137	161
B ₆₄	82	82	35	30	N ₆₄	134	136	137	169
B ₇₁	84	86	17	28	N ₇₁	135	137	148	100
B ₇₂	84	84	17	27	N ₇₂	136	133	146	98
B ₇₃	84	84	17	26	N ₇₃	136	136	145	107
B ₇₄	84	83	17	26	N ₇₄	136	135	144	103
B ₈₁	80	80	53	49	N ₈₁	147	147	121	123
B ₈₂	80	80	53	50	N ₈₂	146	145	122	126
B ₈₃	80	80	53	49	N ₈₃	146	146	122	125
B ₈₄	80	80	53	50	N ₈₄	146	146	123	125
As					As	1815			546

Table 4 NMR parametres of O₂ adsorption on undoped and As-doped of (4, 4) armchair BNNTs, (B) model of Fig.1.

B-11 nuclei	CSI (ppm)		CSA (ppm)		N-14 nuclei	CSI (ppm)		CSA (ppm)	
	Undoped	Doped	Undoped	Doped		Undoped	Doped	Undoped	Doped
B ₁₁	80	84	45	37	N ₁₁	143	146	91	63
B ₁₂	80	80	44	35	N ₁₂	145	142	97	58
B ₁₃	80	80	46	30	N ₁₃	147	147	87	68
B ₁₄	80	80	43	33	N ₁₄	146	146	95	42
B ₂₁	84	86	22	27	N ₂₁	137	114	181	143
B ₂₂	85	83	18	27	N ₂₂	139	136	171	170
B ₂₃	84	84	22	31	N ₂₃	136	135	184	161
B ₂₄	84	84	21	29	N ₂₄	135	139	180	171
B ₃₁	82	70	33	7	N ₃₁	129	123	67	118
B ₃₂	80	82	31	26	N ₃₂	127	113	68	59
B ₃₃	82	81	33	24	N ₃₃	133	133	54	105
B ₃₄	81	83	32	27	N ₃₄	135	135	52	81
B ₄₁	85	85	17	25	N ₄₁ /As	145	-	172	-
B ₄₂	81	72	17	21	N ₄₂	125	138	143	169
B ₄₃	81	81	23	32	N ₄₃	138	140	179	161
B ₄₄	81	82	20	28	N ₄₄	140	143	173	164
B ₅₁	82	63	32	16	N ₅₁	147	119	64	126
B ₅₂	104	83	6	27	N ₅₂	133	124	63	68
B ₅₃	81	81	32	23	N ₅₃	139	139	57	107
B ₅₄	81	83	31	27	N ₅₄	141	141	51	84
B ₆₁	83	84	21	30	N ₆₁	138	113	175	148
B ₆₂	84	82	23	26	N ₆₂	137	135	149	165
B ₆₃	82	82	24	32	N ₆₃	135	134	176	161
B ₆₄	82	82	21	29	N ₆₄	134	136	173	170
B ₇₁	84	87	33	29	N ₇₁	135	137	53	98
B ₇₂	83	85	33	28	N ₇₂	136	133	42	95
B ₇₃	84	84	32	25	N ₇₃	136	136	58	108
B ₇₄	83	84	33	26	N ₇₄	136	135	47	101
B ₈₁	80	80	42	49	N ₈₁	148	148	117	123
B ₈₂	80	80	41	51	N ₈₂	143	145	120	127
B ₈₃	80	80	41	49	N ₈₃	145	146	118	125
B ₈₄	80	80	40	50	N ₈₄	146	146	117	126
As					As		1675		549

Table 5 NMR parametres of O₂ adsorption on undoped and As-doped of (4, 4) armchair BNNTs, (C) model of Fig.1.

B-11 nuclei	CSI (ppm)		CSA (ppm)		N-14 nuclei	CSI (ppm)		CSA (ppm)	
	Undoped	Doped	Undoped	Doped		Undoped	Doped	Undoped	Doped
B ₁₁	81	77	32	16	N ₁₁	146	131	67	77
B ₁₂	80	79	29	14	N ₁₂	146	146	61	87
B ₁₃	81	80	32	18	N ₁₃	146	146	67	74
B ₁₄	81	81	29	22	N ₁₄	146	145	62	69
B ₂₁	84	84	29	30	N ₂₁	136	215	168	47
B ₂₂	85	80	30	30	N ₂₂	136	131	160	140
B ₂₃	84	83	29	35	N ₂₃	136	137	168	134
B ₂₄	85	84	30	35	N ₂₄	136	135	160	138
B ₃₁	83	106	26	19	N ₃₁	135	160	92	96
B ₃₂	81	81	22	19	N ₃₂	135	135	110	86
B ₃₃	83	82	26	16	N ₃₃	135	135	92	130
B ₃₄	81	80	22	13	N ₃₄	135	135	110	141
B ₄₁	79	81	31	31	N ₄₁ /As	114	-	206	-
B ₄₂	81	74	34	15	N ₄₂	135	143	163	151
B ₄₃	79	81	31	33	N ₄₃	114	143	207	134
B ₄₄	81	81	34	35	N ₄₄	135	140	167	140
B ₅₁	79	88	35	13	N ₅₁	139	147	98	97
B ₅₂	77	80	26	19	N ₅₂	138	144	124	101
B ₅₃	79	81	35	36	N ₅₃	140	143	98	132
B ₅₄	77	79	27	12	N ₅₄	138	139	124	146
B ₆₁	79	81	32	32	N ₆₁	105	145	212	108
B ₆₂	80	78	35	37	N ₆₂	128	133	165	146
B ₆₃	80	82	32	33	N ₆₃	104	135	213	128
B ₆₄	80	81	35	36	N ₆₄	128	131	165	135
B ₇₁	85	84	27	17	N ₇₁	137	138	95	130
B ₇₂	83	84	23	18	N ₇₂	134	131	122	154
B ₇₃	85	84	27	15	N ₇₃	137	137	95	140
B ₇₄	83	83	23	17	N ₇₄	134	134	122	154
B ₈₁	81	81	48	51	N ₈₁	146	147	128	115
B ₈₂	80	80	50	49	N ₈₂	145	148	122	122
B ₈₃	81	80	48	52	N ₈₃	146	146	128	118
B ₈₄	80	79	50	54	N ₈₄	145	145	122	122
As					As		1042		1127

Table 6 NMR parametres of O₂ adsorption on undoped and As-doped of (4, 4) armchair BNNTs, (D) model of Fig.1.

B-11 nuclei	CSI (ppm)		CSA (ppm)		N-14 nuclei	CSI (ppm)		CSA (ppm)	
	Undoped	Doped	Undoped	Doped		Undoped	Doped	Undoped	Doped
B ₁₁	80	84	42	23	N ₁₁	143	147	90	67
B ₁₂	80	79	38	21	N ₁₂	142	138	75	100
B ₁₃	80	81	42	16	N ₁₃	147	147	89	81
B ₁₄	80	79	38	23	N ₁₄	145	145	70	90
B ₂₁	83	85	26	32	N ₂₁	137	121	177	79
B ₂₂	83	83	27	34	N ₂₂	135	135	177	124
B ₂₃	84	85	21	34	N ₂₃	135	136	182	117
B ₂₄	84	83	26	35	N ₂₄	136	138	175	110
B ₃₁	84	70	28	11	N ₃₁	133	125	64	115
B ₃₂	79	78	30	17	N ₃₂	129	146	95	75
B ₃₃	82	82	31	12	N ₃₃	135	136	47	140
B ₃₄	81	82	29	8	N ₃₄	134	134	75	155
B ₄₁	79	80	22	26	N ₄₁ /As	99	-	197	-
B ₄₂	79	89	28	28	N ₄₂	139	137	169	125
B ₄₃	81	81	20	35	N ₄₃	141	143	176	122
B ₄₄	81	82	27	36	N ₄₄	133	135	173	115
B ₅₁	106	121	22	24	N ₅₁	169	172	30	132
B ₅₂	79	78	29	12	N ₅₂	134	140	103	116
B ₅₃	82	82	30	12	N ₅₃	142	142	51	142
B ₅₄	80	80	28	9	N ₅₄	140	141	79	155
B ₆₁	79	81	23	34	N ₆₁	140	136	159	97
B ₆₂	78	80	30	36	N ₆₂	133	130	173	121
B ₆₃	81	82	21	34	N ₆₃	136	137	174	122
B ₆₄	81	82	27	36	N ₆₄	127	126	173	112
B ₇₁	85	87	28	18	N ₇₁	135	138	22	137
B ₇₂	83	83	30	9	N ₇₂	131	128	85	172
B ₇₃	84	84	31	15	N ₇₃	137	138	55	146
B ₇₄	83	83	30	9	N ₇₄	135	135	81	170
B ₈₁	80	80	41	53	N ₈₁	145	147	121	123
B ₈₂	80	80	46	53	N ₈₂	146	145	119	116
B ₈₃	80	80	41	52	N ₈₃	147	147	121	119
B ₈₄	80	80	46	53	N ₈₄	147	146	116	113
As					As		75		1229

of ^{14}N nuclei at the N21, N32, N51 and N61 sites of As-doped decrease significantly from undoped model. In addition, the CSA values of ^{14}N nuclei at the layers 1, 4, 6 decrease and other layers increase. The results of Table 5 for C models reveal that the CSI values of ^{11}B

nuclei with As-doped at the B42 site decrease largely from 81 to 74 ppm and at sites B31 and B52 increase from 83, 77 ppm to 106 and 80 respectively. The CSA value of ^{11}B nuclei at the layers 1, 3, 7 decreases from undoped model and the other sites increase. The CSI values of

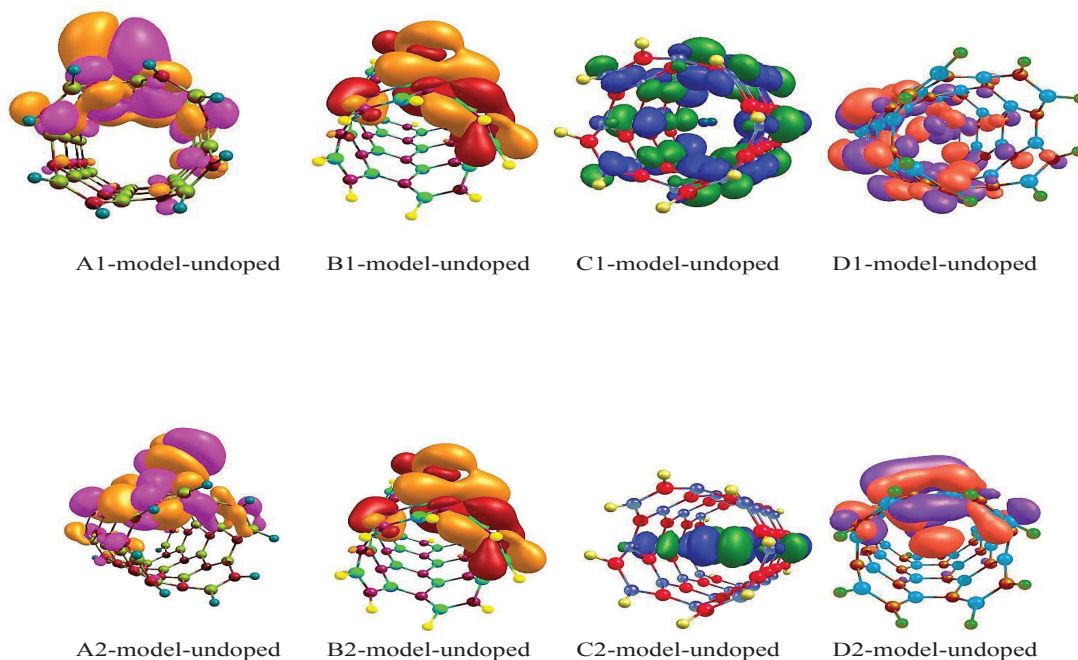


Fig. 3 Comparisons the HOMO-LUMO structures of O_2 adsorption on the undoped of (4,4) armchair model of BNNTs, index (1) used for HOMO and index (2) for LUMO (A-D) models (see Fig.1).

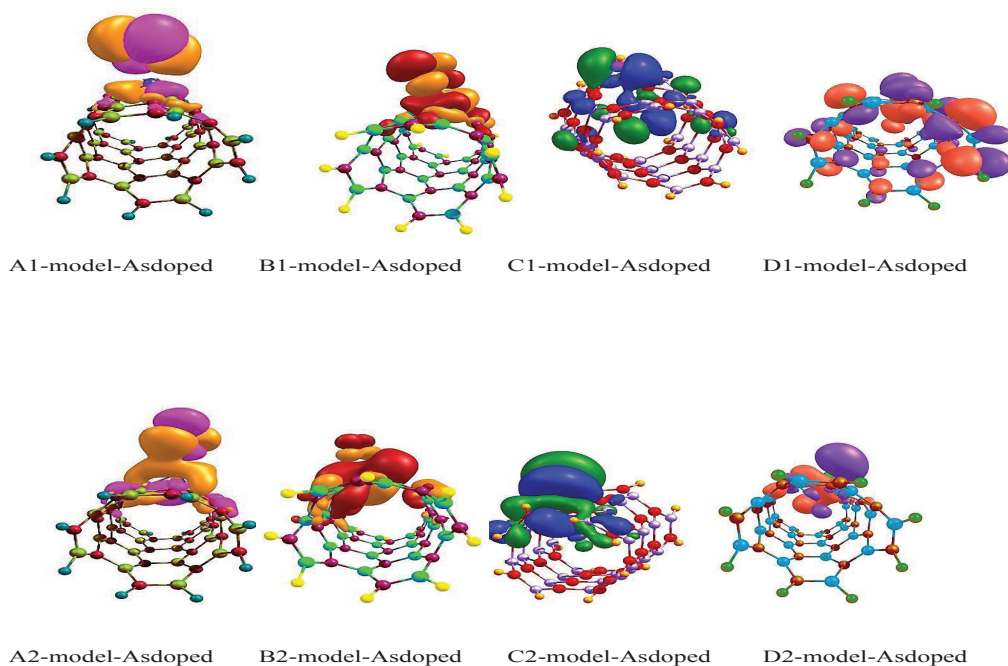


Fig. 4 Comparisons the HOMO-LUMO structures of O_2 adsorption on the As-doped of (4,4) armchair model of BNNTs, index (1) used for HOMO and index (2) for LUMO (A-D) models (see Fig.2).

^{14}N nuclei at the N21, N31, N43, N52, N61, and N63 sites increase from undoped model. The CSA values of ^{14}N nuclei at the layers 2, 4, 6, 8 decrease from undoped model and the other layers increase. The calculated results of D model (Table 6) show that the CSI values of ^{11}B nuclei with As-doped at B42 and B51 sites increase from 79, 106 ppm to 89, 121 ppm, and at site B31 decrease from 84 to 76 ppm. CSA values of ^{11}B nuclei at odd layers decrease and even layers increase from undoped models. On the other hand, the CSI values of ^{14}N nuclei at the sites N21, N31 and N61 decrease and at sites N32, N51 and N52 increase from undoped model. In addition, the CSA values of ^{14}N nuclei at even layers decrease and at layers 3, 5, 7 increase significantly from undoped models. The comparison results show that the CSI and CSA values depended on either As-doped or configurations of O_2 adsorption.

4. Conclusions

In this research we studied the adsorptions of O_2 gas on four models of the outer and inner surface of pristine and As-doped (4, 4) armchair BNNTs by means of density functional theory (DFT) calculations. The results reveal that adsorption energy of undoped of nanotube in four models are exothermic and at the (A and B) models are more than other models, so the adsorption O_2 on surface of these models are favorable than other models. With doping As in all models the adsorption energy is decrease. The gap energy between LUMO-MOMO orbital with adsorbing O_2 gas on the surface of nanotube decrease and so the conductivity properties of nanotube are increase. The gap energy of undoped C model is lower than other models. The comparing results of quantum properties reveal that the global hardness, electronic chemical potential and stability of

nanotube are decrease and so the reactivity of the O_2 adsorbed is increase. The comparison results of NMR parameters show that the CSI and CSA values depended on either As-doped or configurations of O_2 adsorption.

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